



Series WX1YZ/4



SET ~ 1

प्रश्न-पत्र कोड
Q.P. Code

30/4/1

रोल नं.

Roll No.

--	--	--	--	--	--	--	--

परीक्षार्थी प्रश्न-पत्र कोड को उत्तर-पुस्तिका के मुख-पृष्ठ पर अवश्य लिखें।

Candidates must write the Q.P. Code on the title page of the answer-book.

गणित (मानक) – सैद्धान्तिक

MATHEMATICS (STANDARD) - Theory

#

निर्धारित समय : 3 घण्टे
Time allowed : 3 hours

अधिकतम अंक : 80
Maximum Marks : 80

नोट / NOTE :

(i) कृपया जाँच कर लें कि इस प्रश्न-पत्र में मुद्रित पृष्ठ 15 हैं।

Please check that this question paper contains 15 printed pages.

(ii) प्रश्न-पत्र में दाहिने हाथ की ओर दिए गए प्रश्न-पत्र कोड को छात्र उत्तर-पुस्तिका के मुख-पृष्ठ पर लिखें।

Q.P. Code given on the right hand side of the question paper should be written on the title page of the answer-book by the candidate.

(iii) कृपया जाँच कर लें कि इस प्रश्न-पत्र में 38 प्रश्न हैं।

Please check that this question paper contains 38 questions.

(iv) कृपया प्रश्न का उत्तर लिखना शुरू करने से पहले, उत्तर-पुस्तिका में प्रश्न का क्रमांक अवश्य लिखें।

Please write down the Serial Number of the question in the answer-book before attempting it.

(v) इस प्रश्न-पत्र को पढ़ने के लिए 15 मिनट का समय दिया गया है। प्रश्न-पत्र का वितरण पूर्वाह्न में 10.15 बजे किया जाएगा। 10.15 बजे से 10.30 बजे तक छात्र केवल प्रश्न-पत्र को पढ़ेंगे और इस अवधि के दौरान वे उत्तर-पुस्तिका पर कोई उत्तर नहीं लिखेंगे।

15 minute time has been allotted to read this question paper. The question paper will be distributed at 10.15 a.m. From 10.15 a.m. to 10.30 a.m., the students will read the question paper only and will not write any answer on the answer-book during this period.



GENERAL INSTRUCTIONS :

Read the following instructions carefully and follow them :

- (i) This question paper contains **38** questions. All questions are compulsory.
- (ii) Question paper is divided into **FIVE** sections – **Section A, B, C, D and E**.
- (iii) In **section A** – question number **1** to **18** are multiple choice questions (MCQs) and question number **19** and **20** are Assertion-Reason based questions of **1** mark each.
- (iv) In **section B** – question number **21** to **25** are Very Short Answer (VSA) type questions of **2** marks each.
- (v) In **section C** – question number **26** to **31** are Short Answer (SA) type questions carrying **3** marks each.
- (vi) In **section D** – question number **32** to **35** are Long Answer (LA) type questions carrying **5** marks each.
- (vii) In **section E** – question number **36** to **38** are **case based integrated units** of assessment questions carrying **4** marks each. Internal choice is provided in **2** marks question in each case-study.
- (viii) There is no overall choice. However, an internal choice has been provided in **2** questions in **Section B**, **2** questions in **Section C**, **2** questions in **Section D** and **3** questions in **Section E**.
- (ix) Draw neat figures wherever required. Take $\pi = 22/7$ wherever required if not stated.
- (x) Use of calculators is **NOT allowed**.

SECTION - A

Section - A consists of Multiple Choice type questions of 1 mark each.

1. The ratio of HCF to LCM of the least composite number and the least prime number is : 1
(a) 1:2 (b) 2:1 (c) 1:1 (d) 1:3

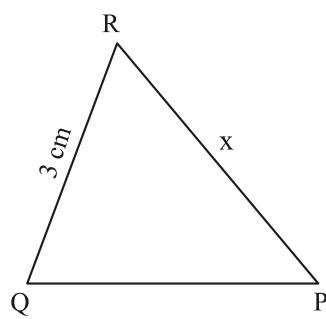
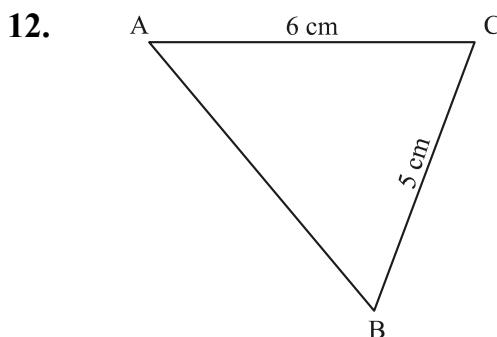
2. The roots of the equation $x^2 + 3x - 10 = 0$ are : 1
(a) 2, -5 (b) -2, 5 (c) 2, 5 (d) -2, -5

3. The next term of the A.P. : $\sqrt{6}$, $\sqrt{24}$, $\sqrt{54}$ is : 1
(a) $\sqrt{60}$ (b) $\sqrt{96}$ (c) $\sqrt{72}$ (d) $\sqrt{216}$

4. The distance of the point (-1, 7) from x-axis is : 1
(a) -1 (b) 7 (c) 6 (d) $\sqrt{50}$

5. What is the area of a semi-circle of diameter 'd' ? 1
(a) $\frac{1}{16}\pi d^2$ (b) $\frac{1}{4}\pi d^2$ (c) $\frac{1}{8}\pi d^2$ (d) $\frac{1}{2}\pi d^2$

6. The empirical relation between the mode, median and mean of a distribution is : 1
(a) Mode = 3 Median - 2 Mean (b) Mode = 3 Mean - 2 Median
(c) Mode = 2 Median - 3 Mean (d) Mode = 2 Mean - 3 Median

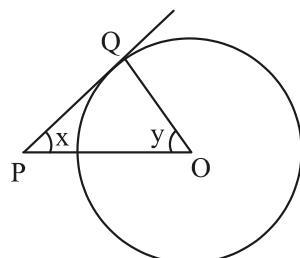


In the given figure, $\triangle ABC \sim \triangle QPR$. If $AC = 6 \text{ cm}$, $BC = 5 \text{ cm}$, $QR = 3 \text{ cm}$ and $PR = x$; then the value of x is :

(a) 3.6 cm (b) 2.5 cm (c) 10 cm (d) 3.2 cm

13. The distance of the point $(-6, 8)$ from origin is : 1
 (a) 6 (b) -6 (c) 8 (d) 10

14. In the given figure, PQ is a tangent to the circle with centre O . If $\angle OPQ = x$, $\angle POQ = y$, then $x + y$ is : 1
 (a) 45°
 (b) 90°
 (c) 60°
 (d) 180°

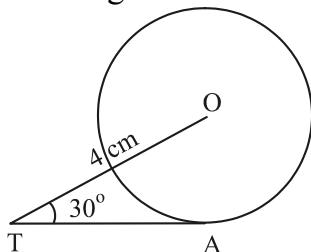




15. In the given figure, TA is a tangent to the circle with centre O such that $OT = 4 \text{ cm}$, $\angle OTA = 30^\circ$, then length of TA is :

1

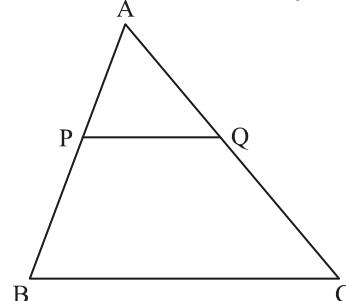
- (a) $2\sqrt{3} \text{ cm}$
- (b) 2 cm
- (c) $2\sqrt{2} \text{ cm}$
- (d) $\sqrt{3} \text{ cm}$



16. In $\triangle ABC$, $PQ \parallel BC$. If $PB = 6 \text{ cm}$, $AP = 4 \text{ cm}$, $AQ = 8 \text{ cm}$, find the length of AC.

1

- (a) 12 cm
- (b) 20 cm
- (c) 6 cm
- (d) 14 cm



17. If α, β are the zeroes of the polynomial $p(x) = 4x^2 - 3x - 7$, then

1

$$\left(\frac{1}{\alpha} + \frac{1}{\beta} \right)$$

- (a) $\frac{7}{3}$
- (b) $-\frac{7}{3}$
- (c) $\frac{3}{7}$
- (d) $-\frac{3}{7}$

18. A card is drawn at random from a well-shuffled pack of 52 cards. The probability that the card drawn is not an ace is :

1

- (a) $\frac{1}{13}$
- (b) $\frac{9}{13}$
- (c) $\frac{4}{13}$
- (d) $\frac{12}{13}$

DIRECTIONS : In the question number **19** and **20**, a statement of **Assertion (A)** is followed by a statement of **Reason (R)**. Choose the correct option out of the following :

19. **Assertion (A) :** The probability that a leap year has 53 Sundays is $\frac{2}{7}$.

1

Reason (R) : The probability that a non-leap year has 53 Sundays is $\frac{5}{7}$.

- (a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).
- (b) Both Assertion (A) and Reason (R) are true and Reason (R) is not the correct explanation of Assertion (A).
- (c) Assertion (A) is true but Reason (R) is false.
- (d) Assertion (A) is false but Reason (R) is true.





20. **Assertion (A) :** a, b, c are in A.P. if and only if $2b = a + c$.
Reason (R) : The sum of first n odd natural numbers is n^2 . 1

(a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).
(b) Both Assertion (A) and Reason (R) are true and Reason (R) is not the correct explanation of Assertion (A).
(c) Assertion (A) is true but Reason (R) is false.
(d) Assertion (A) is false but Reason (R) is true.

SECTION – B

Section - B consists of Very Short Answer (VSA) type questions of 2 marks each.

21. Two numbers are in the ratio 2 : 3 and their LCM is 180. What is the HCF of these numbers ? 2

22. If one zero of the polynomial $p(x) = 6x^2 + 37x - (k - 2)$ is reciprocal of the other, then find the value of k. 2

23. (A) Find the sum and product of the roots of the quadratic equation $2x^2 - 9x + 4 = 0$. 2

OR

(B) Find the discriminant of the quadratic equation $4x^2 - 5 = 0$ and hence comment on the nature of roots of the equation. 2

24. If a fair coin is tossed twice, find the probability of getting ‘atmost one head’. 2

25. (A) Evaluate
$$\frac{5\cos^2 60^\circ + 4\sec^2 30^\circ - \tan^2 45^\circ}{\sin^2 30^\circ + \cos^2 30^\circ}$$
 2

OR

(B) If A and B are acute angles such that $\sin(A - B) = 0$ and $2 \cos(A + B) - 1 = 0$, then find angles A and B. 2

SECTION – C

Section - C consists of Short Answer (SA) type questions of 3 marks each.

26. (A) How many terms are there in an A.P. whose first and fifth terms are – 14 and 2, respectively and the last term is 62. 3

OR

(B) Which term of the A.P. : 65, 61, 57, 53, is the first negative term ? 3

27. Prove that $\sqrt{5}$ is an irrational number. 3

28. Prove that the angle between the two tangents drawn from an external point to a circle is supplementary to the angle subtended by the line-segment joining the points of contact at the centre. 3





29. (A) Prove that $\frac{\sin A - 2 \sin^3 A}{2 \cos^3 A - \cos A} = \tan A$ 3

OR

(B) Prove that $\sec A (1 - \sin A) (\sec A + \tan A) = 1$. 3

30. Two concentric circles are of radii 5 cm and 3 cm. Find the length of the chord of the larger circle which touches the smaller circle. 3

31. Find the value of 'p' for which the quadratic equation $px(x - 2) + 6 = 0$ has two equal real roots. 3

SECTION – D

Section - D consists of Long Answer (LA) type questions of 5 marks each.

32. (A) A straight highway leads to the foot of a tower. A man standing on the top of the 75 m high tower observes two cars at angles of depression of 30° and 60° , which are approaching the foot of the tower. If one car is exactly behind the other on the same side of the tower, find the distance between the two cars. (use $\sqrt{3} = 1.73$) 5

OR

(B) From the top of a 7 m high building, the angle of elevation of the top of a cable tower is 60° and the angle of depression of its foot is 30° . Determine the height of the tower. 5

33. (A) D is a point on the side BC of a triangle ABC such that $\angle ADC = \angle BAC$, prove that $CA^2 = CB \cdot CD$ 5

OR

(B) If AD and PM are medians of triangles ABC and PQR, respectively where $\Delta ABC \sim \Delta PQR$, prove that $\frac{AB}{PQ} = \frac{AD}{PM}$. 5

34. A student was asked to make a model shaped like a cylinder with two cones attached to its ends by using a thin aluminium sheet. The diameter of the model is 3 cm and its total length is 12 cm. If each cone has a height of 2 cm, find the volume of air contained in the model. 5

35. The monthly expenditure on milk in 200 families of a Housing Society is given below :

Monthly Expenditure (in ₹)	1000-1500	1500-2000	2000-2500	2500-3000	3000-3500	3500-4000	4000-4500	4500-5000
Number of families	24	40	33	x	30	22	16	7

Find the value of x and also, find the median and mean expenditure on milk.

5





SECTION – E

Section – E consists of three Case Study Based questions of 4 marks each.

36. Two schools ‘P’ and ‘Q’ decided to award prizes to their students for two games of Hockey ₹ x per student and Cricket ₹ y per student. School ‘P’ decided to award a total of ₹ 9,500 for the two games to 5 and 4 students respectively; while school ‘Q’ decided to award ₹ 7,370 for the two games to 4 and 3 students respectively.



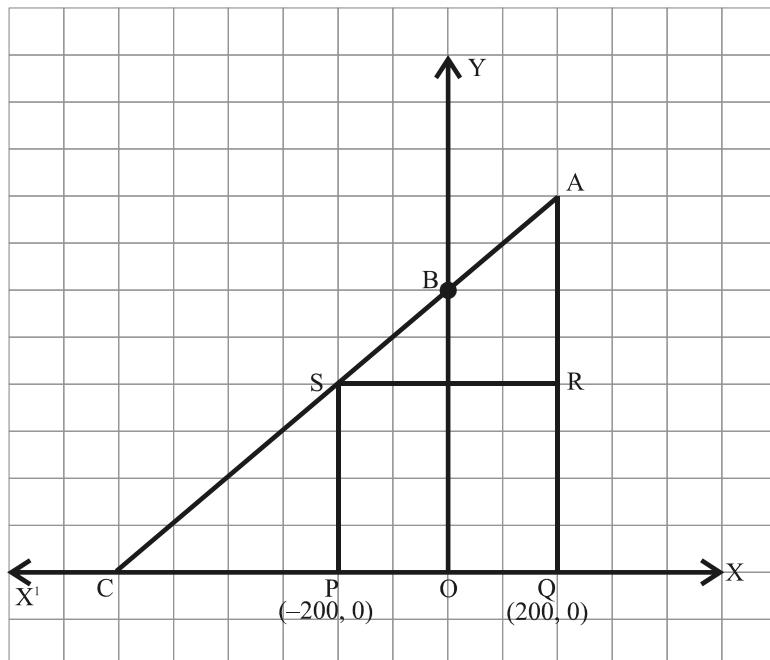
Based on the above information, answer the following questions :

(i) Represent the following information algebraically (in terms of x and y). 1
(ii) (a) What is the prize amount for hockey ? 2

OR

(b) Prize amount on which game is more and by how much ? 2
(iii) What will be the total prize amount if there are 2 students each from two games ? 1

37. Jagdish has a field which is in the shape of a right angled triangle AQC. He wants to leave a space in the form of a square PQRS inside the field for growing wheat and the remaining for growing vegetables (as shown in the figure). In the field, there is a pole marked as O.



Based on the above information, answer the following questions :

(i) Taking O as origin, coordinates of P are $(-200, 0)$ and of Q are $(200, 0)$. PQRS being a square, what are the coordinates of R and S ? 1





(ii) (a) What is the area of square PQRS ?

2

OR

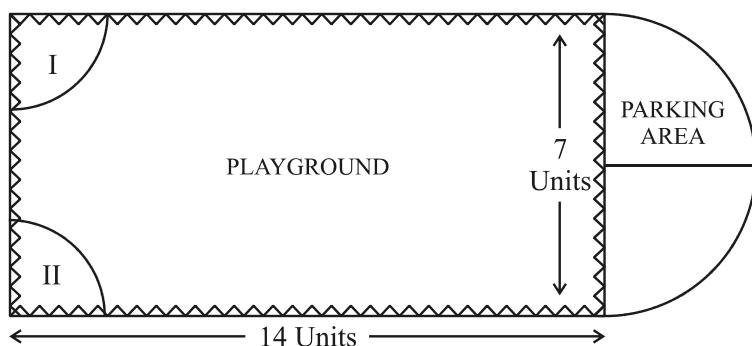
(b) What is the length of diagonal PR in square PQRS ?

2

(iii) If S divides CA in the ratio K:1, what is the value of K, where point A is (200, 800) ?

1

38. Governing council of a local public development authority of Dehradun decided to build an adventurous playground on the top of a hill, which will have adequate space for parking.



After survey, it was decided to build rectangular playground, with a semi-circular area allotted for parking at one end of the playground. The length and breadth of the rectangular playground are 14 units and 7 units, respectively. There are two quadrants of radius 2 units on one side for special seats.

Based on the above information, answer the following questions :

(i) What is the total perimeter of the parking area ?

1

(ii) (a) What is the total area of parking and the two quadrants ?

2

OR

(b) What is the ratio of area of playground to the area of parking area ?

2

(iii) Find the cost of fencing the playground and parking area at the rate of ₹ 2 per unit.

1



Marking Scheme
Strictly Confidential
(For Internal and Restricted use only)
Secondary School Examination, 2023
MATHEMATICS PAPER CODE 30/4/1

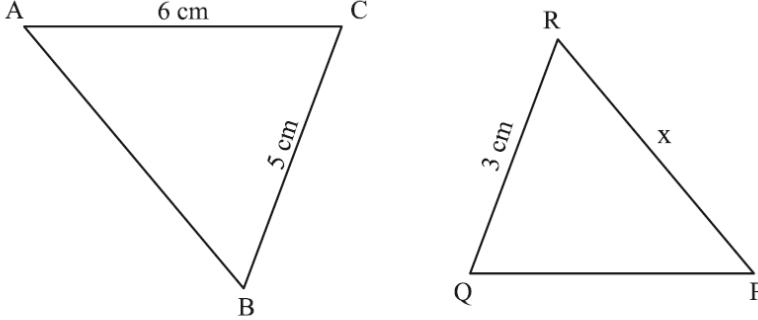
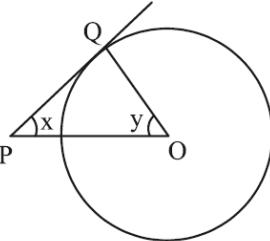
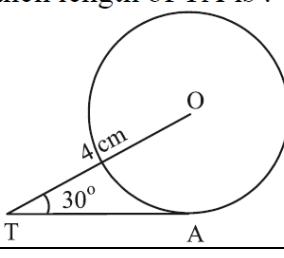
General Instructions: -

1	You are aware that evaluation is the most important process in the actual and correct assessment of the candidates. A small mistake in evaluation may lead to serious problems which may affect the future of the candidates, education system and teaching profession. To avoid mistakes, it is requested that before starting evaluation, you must read and understand the spot evaluation guidelines carefully.
2	“Evaluation policy is a confidential policy as it is related to the confidentiality of the examinations conducted, Evaluation done and several other aspects. Its’ leakage to public in any manner could lead to derailment of the examination system and affect the life and future of millions of candidates. Sharing this policy/document to anyone, publishing in any magazine and printing in News Paper/Website etc may invite action under various rules of the Board and IPC.”
3	Evaluation is to be done as per instructions provided in the Marking Scheme. It should not be done according to one’s own interpretation or any other consideration. Marking Scheme should be strictly adhered to and religiously followed. However, while evaluating, answers which are based on latest information or knowledge and/or are innovative, they may be assessed for their correctness otherwise and due marks be awarded to them.
4	The Marking scheme carries only suggested value points for the answers. These are in the nature of Guidelines only and do not constitute the complete answer. The students can have their own expression and if the expression is correct, the due marks should be awarded accordingly.
5	The Head-Examiner must go through the first five answer books evaluated by each evaluator on the first day, to ensure that evaluation has been carried out as per the instructions given in the Marking Scheme. If there is any variation, the same should be zero after deliberation and discussion. The remaining answer books meant for evaluation shall be given only after ensuring that there is no significant variation in the marking of individual evaluators.
6	Evaluators will mark (✓) wherever answer is correct. For wrong answer CROSS ‘X’ be marked. Evaluators will not put right (✓) while evaluating which gives an impression that answer is correct and no marks are awarded. This is most common mistake which evaluators are committing.
7	If a question has parts, please award marks on the right-hand side for each part. Marks awarded for different parts of the question should then be totaled up and written in the left-hand margin and encircled. This may be followed strictly.
8	If a question does not have any parts, marks must be awarded in the left-hand margin and encircled. This may also be followed strictly.
9	<u>In Q1-Q20, if a candidate attempts the question more than once (without canceling the previous attempt), marks shall be awarded for the first attempt only and the other answer scored out with a note “Extra Question”.</u>
10	<u>In Q21-Q38, if a student has attempted an extra question, answer of the question deserving more marks should be retained and the other answer scored out with a note “Extra Question”.</u>
11	No marks to be deducted for the cumulative effect of an error. It should be penalized only once.
12	A full scale of marks _____ (example 0 to 80/70/60/50/40/30 marks as given in Question Paper) has to be used. Please do not hesitate to award full marks if the answer deserves it.

13	Every examiner has to necessarily do evaluation work for full working hours i.e., 8 hours every day and evaluate 20 answer books per day in main subjects and 25 answer books per day in other subjects (Details are given in Spot Guidelines). This is in view of the reduced syllabus and number of questions in question paper.
14	<p>Ensure that you do not make the following common types of errors committed by the Examiner in the past:-</p> <ul style="list-style-type: none"> • Leaving answer or part thereof unassessed in an answer book. • Giving more marks for an answer than assigned to it. • Wrong totaling of marks awarded on an answer. • Wrong transfer of marks from the inside pages of the answer book to the title page. • Wrong question wise totaling on the title page. • Wrong totaling of marks of the two columns on the title page. • Wrong grand total. • Marks in words and figures not tallying/not same. • Wrong transfer of marks from the answer book to online award list. • Answers marked as correct, but marks not awarded. (Ensure that the right tick mark is correctly and clearly indicated. It should merely be a line. Same is with the X for incorrect answer.) • Half or a part of answer marked correct and the rest as wrong, but no marks awarded.
15	While evaluating the answer books if the answer is found to be totally incorrect, it should be marked as cross (X) and awarded zero (0) Marks.
16	Any un assessed portion, non-carrying over of marks to the title page, or totaling error detected by the candidate shall damage the prestige of all the personnel engaged in the evaluation work as also of the Board. Hence, in order to uphold the prestige of all concerned, it is again reiterated that the instructions be followed meticulously and judiciously.
17	The Examiners should acquaint themselves with the guidelines given in the " Guidelines for spot Evaluation " before starting the actual evaluation.
18	Every Examiner shall also ensure that all the answers are evaluated, marks carried over to the title page, correctly totaled and written in figures and words.
19	The candidates are entitled to obtain photocopy of the Answer Book on request on payment of the prescribed processing fee. All Examiners/Additional Head Examiners/Head Examiners are once again reminded that they must ensure that evaluation is carried out strictly as per value points for each answer as given in the Marking Scheme.

MARKING SCHEME
MATHEMATICS (Subject Code-041)
(PAPER CODE: 30/4/1)

Q. No.	EXPECTED OUTCOMES/VALUE POINTS	Marks
	SECTION A Questions no. 1 to 18 are multiple choice questions (MCQs) and questions number 19 and 20 are Assertion-Reason based questions of 1 mark each	
1.	The ratio of HCF to LCM of the least composite number and the least prime number is : (a) 1:2 (b) 2:1 (c) 1:1 (d) 1:3	
Sol.	(a) 1 : 2	1
2.	The roots of the equation $x^2 + 3x - 10 = 0$ are : (a) 2, -5 (b) -2, 5 (c) 2, 5 (d) -2, -5	
Sol.	(a) 2, -5	1
3.	The next term of the A.P. : $\sqrt{6}$, $\sqrt{24}$, $\sqrt{54}$ is : (a) $\sqrt{60}$ (b) $\sqrt{96}$ (c) $\sqrt{72}$ (d) $\sqrt{216}$	
Sol.	(b) $\sqrt{96}$	1
4.	The distance of the point (-1, 7) from x-axis is : (a) -1 (b) 7 (c) 6 (d) $\sqrt{50}$	
Sol.	(b) 7	1
5.	What is the area of a semi-circle of diameter 'd' ? (a) $\frac{1}{16}\pi d^2$ (b) $\frac{1}{4}\pi d^2$ (c) $\frac{1}{8}\pi d^2$ (d) $\frac{1}{2}\pi d^2$	
Sol.	(c) $\frac{1}{8}\pi d^2$	1
6.	The empirical relation between the mode, median and mean of a distribution is : (a) Mode = 3 Median - 2 Mean (b) Mode = 3 Mean - 2 Median (c) Mode = 2 Median - 3 Mean (d) Mode = 2 Mean - 3 Median	

12.	 <p>In the given figure, $\triangle ABC \sim \triangle QPR$. If $AC = 6 \text{ cm}$, $BC = 5 \text{ cm}$, $QR = 3 \text{ cm}$ and $PR = x$; then the value of x is :</p> <p>(a) 3.6 cm (b) 2.5 cm (c) 10 cm (d) 3.2 cm</p>	
Sol.	(b) 2.5 cm	1
13.	<p>The distance of the point $(-6, 8)$ from origin is :</p> <p>(a) 6 (b) -6 (c) 8 (d) 10</p>	
Sol.	(d) 10	1
14.	<p>In the given figure, PQ is a tangent to the circle with centre O. If $\angle OPQ = x$, $\angle POQ = y$, then $x + y$ is :</p> <p>(a) 45° (b) 90° (c) 60° (d) 180°</p> 	
Sol.	(b) 90°	1
15.	<p>In the given figure, TA is a tangent to the circle with centre O such that $OT = 4 \text{ cm}$, $\angle OTA = 30^\circ$, then length of TA is :</p> <p>(a) $2\sqrt{3} \text{ cm}$ (b) 2 cm (c) $2\sqrt{2} \text{ cm}$ (d) $\sqrt{3} \text{ cm}$</p> 	
Sol.	(a) $2\sqrt{3} \text{ cm}$	1

16.	<p>In $\triangle ABC$, $PQ \parallel BC$. If $PB = 6$ cm, $AP = 4$ cm, $AQ = 8$ cm, find the length of AC.</p> <p>(a) 12 cm (b) 20 cm (c) 6 cm (d) 14 cm</p>	
Sol.	(b) 20 cm	1
17.	<p>If α, β are the zeroes of the polynomial $p(x) = 4x^2 - 3x - 7$, then $\left(\frac{1}{\alpha} + \frac{1}{\beta}\right)$ is equal to :</p> <p>(a) $\frac{7}{3}$ (b) $-\frac{7}{3}$ (c) $\frac{3}{7}$ (d) $-\frac{3}{7}$</p>	
Sol.	(d) $-\frac{3}{7}$	1
18.	<p>A card is drawn at random from a well-shuffled pack of 52 cards. The probability that the card drawn is not an ace is :</p> <p>(a) $\frac{1}{13}$ (b) $\frac{9}{13}$ (c) $\frac{4}{13}$ (d) $\frac{12}{13}$</p>	
Sol.	(d) $\frac{12}{13}$	1
	<p>DIRECTIONS : In the question number 19 and 20, a statement of Assertion (A) is followed by a statement of Reason (R). Choose the correct option out of the following :</p>	

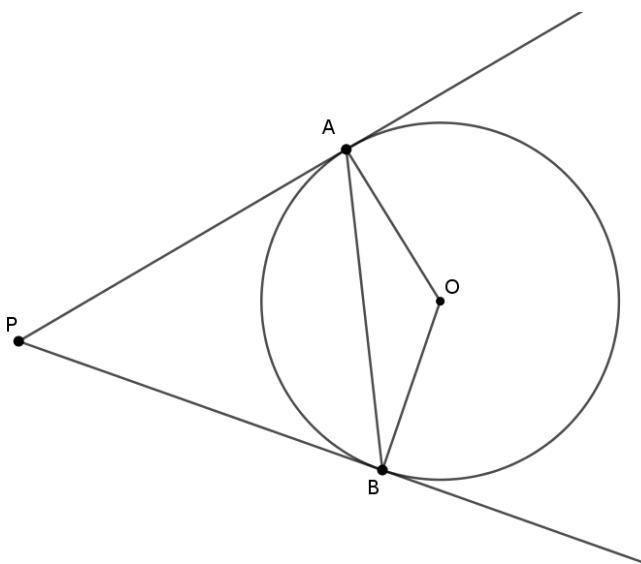
19.	<p>Assertion (A) : The probability that a leap year has 53 Sundays is $\frac{2}{7}$.</p> <p>Reason (R) : The probability that a non-leap year has 53 Sundays is $\frac{5}{7}$.</p> <p>(a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).</p> <p>(b) Both Assertion (A) and Reason (R) are true and Reason (R) is not the correct explanation of Assertion (A).</p> <p>(c) Assertion (A) is true but Reason (R) is false.</p> <p>(d) Assertion (A) is false but Reason (R) is true.</p>	
Sol.	(c) Assertion (A) is true but Reason (R) is false	1
20.	<p>Assertion (A) : a, b, c are in A.P. if and only if $2b = a + c$.</p> <p>Reason (R) : The sum of first n odd natural numbers is n^2.</p> <p>(a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).</p> <p>(b) Both Assertion (A) and Reason (R) are true and Reason (R) is not the correct explanation of Assertion (A).</p> <p>(c) Assertion (A) is true but Reason (R) is false.</p> <p>(d) Assertion (A) is false but Reason (R) is true.</p>	
Sol.	(b) Both Assertion (A) and Reason (R) are true and Reason (R) is not the correct explanation of Assertion (A).	1
	<p>SECTION B</p> <p>This section comprises very short answer (VSA) type questions of 2 marks each.</p>	
21.	Two numbers are in the ratio 2 : 3 and their LCM is 180. What is the HCF of these numbers ?	
Sol.	<p>Let the numbers be $2x, 3x$</p> <p>$LCM = 6x = 180 \Rightarrow x = 30$</p> <p>$\therefore$ Numbers are 60, 90</p> <p>$HCF(60, 90) = 30$</p>	<p>1</p> <p>1</p>
22.	If one zero of the polynomial $p(x) = 6x^2 + 37x - (k - 2)$ is reciprocal of the other, then find the value of k.	

Sol.	$p(x) = 6x^2 + 37x - (k - 2)$ <p>Let the zeroes be $\alpha, \frac{1}{\alpha}$</p> <p>Product of zeroes = $\alpha \cdot \frac{1}{\alpha} = -\frac{(k - 2)}{6}$</p> $6 = -k + 2 \Rightarrow k = -4$	$\frac{1}{2}$ 1 $\frac{1}{2}$
23(A).	Find the sum and product of the roots of the quadratic equation $2x^2 - 9x + 4 = 0$.	
Sol.	$2x^2 - 9x + 4 = 0$ <p>$a = 2, b = -9, c = 4$</p> <p>Let α, β be roots of $2x^2 - 9x + 4 = 0$</p> <p>Sum = $\alpha + \beta = -\frac{b}{a} = -\frac{9}{2}$</p> <p>Product of roots = $\alpha\beta = \frac{c}{a} = \frac{4}{2} = 2$</p>	1 1
OR		
23(B).	Find the discriminant of the quadratic equation $4x^2 - 5 = 0$ and hence comment on the nature of roots of the equation.	
Sol.	$4x^2 - 5 = 0$ <p>$a = 4, b = 0, c = -5$</p> <p>Discriminant = $b^2 - 4ac = 0 - 4(4)(-5) = 80 > 0$</p> <p>$\Rightarrow$ roots are real and distinct.</p>	$1\frac{1}{2}$ $\frac{1}{2}$
24.	If a fair coin is tossed twice, find the probability of getting 'atmost one head'.	

Sol.	<p>Total outcomes are HH, HT, TH, TT Favourable outcomes are HT, TH, TT $P(\text{at most one head}) = \frac{3}{4}$</p>	$\frac{1}{2}$ $\frac{1}{2}$ 1
25(A).	Evaluate $\frac{5 \cos^2 60^\circ + 4 \sec^2 30^\circ - \tan^2 45^\circ}{\sin^2 30^\circ + \cos^2 30^\circ}$	
Sol.	$\frac{5 \cos^2 60^\circ + 4 \sec^2 30^\circ - \tan^2 45^\circ}{\sin^2 30^\circ + \cos^2 30^\circ}$ $= \frac{5(1/2)^2 + 4(2/\sqrt{3})^2 - (1)^2}{1}$ $= \frac{5/4 + 16/3 - 1}{1} = \frac{67}{12}$	$\frac{1}{2}$ $\frac{1}{2}$
OR	OR	
25(B).	If A and B are acute angles such that $\sin(A - B) = 0$ and $2 \cos(A + B) - 1 = 0$, then find angles A and B.	
Sol.	$\sin(A - B) = 0 \Rightarrow A - B = 0^\circ$ $\cos(A + B) = \frac{1}{2} \Rightarrow A + B = 60^\circ$ $\Rightarrow A = 30^\circ, B = 30^\circ$	$\frac{1}{2}$ $\frac{1}{2}$ 1
SECTION C	This section comprises of Short Answer (SA) type questions of 3 marks each.	
26(A).	How many terms are there in an A.P. whose first and fifth terms are -14 and 2, respectively and the last term is 62.	

Sol.	$a = -14, a_5 = 2 \Rightarrow a + 4d = 2$ $-14 + 4d = 2 \Rightarrow d = 4$ $a_n = 62 \Rightarrow a + (n-1)d = 62$ $-14 + (n-1)4 = 62 \Rightarrow n = 20$	1 1 1
26(B).	OR	
	<p>Which term of the A.P. : 65, 61, 57, 53, is the first negative term ?</p> <p>Sol.</p> <p>65, 61, 57, 53, ...</p> <p>$a = 65, d = -4$</p> <p>Let a_n be the first negative term</p> $a_n < 0 \Rightarrow a + (n-1)d < 0$ $65 + (n-1)(-4) < 0 \Rightarrow 69 - 4n < 0$ $n > \frac{69}{4}$ <p>\therefore Least positive integral value of n which satisfies $n > \frac{69}{4}$ is 18</p> <p>\therefore 1st negative term of the AP = 18</p>	1 1 1 1 1 1
27.	Prove that $\sqrt{5}$ is an irrational number.	
Sol.	<p>Let $\sqrt{5}$ be a rational number.</p> <p>$\therefore \sqrt{5} = \frac{p}{q}$, where $q \neq 0$ and let p & q be co-primes.</p> <p>$5q^2 = p^2 \Rightarrow p^2$ is divisible by 5 $\Rightarrow p$ is divisible by 5</p> <p>$\Rightarrow p = 5a$, where 'a' is some integer ----- (i)</p> <p>$25a^2 = 5q^2 \Rightarrow q^2 = 5a^2 \Rightarrow q^2$ is divisible by 5 $\Rightarrow q$ is divisible by 5</p> <p>$\Rightarrow q = 5b$, where 'b' is some integer ----- (ii)</p> <p>(i) and (ii) leads to contradiction as 'p' and 'q' are co-primes.</p> <p>$\therefore \sqrt{5}$ is an irrational number.</p>	1/2 1 1/2 1
28.	Prove that the angle between the two tangents drawn from an external point to a circle is supplementary to the angle subtended by the line-segment joining the points of contact at the centre.	

Sol. PA and PB are tangents drawn from the external point P to the circle with centre O.



**1 mark
for
correct
figure**

In quad. OAPB,

$$\angle OAP + \angle APB + \angle OBP + \angle AOB = 360^\circ$$

1

$$90^\circ + \angle APB + 90^\circ + \angle AOB = 360^\circ \text{ (Tangent } \perp \text{ radius)}$$

$\frac{1}{2}$

$$\angle APB + \angle AOB = 360^\circ - 180^\circ = 180^\circ$$

$\frac{1}{2}$

29(A).

$$\text{Prove that } \frac{\sin A - 2 \sin^3 A}{2 \cos^3 A - \cos A} = \tan A$$

Sol.

$$\text{LHS} = \frac{\sin A - 2 \sin^3 A}{2 \cos^3 A - \cos A} = \frac{\sin A (1 - 2 \sin^2 A)}{\cos A (2 \cos^2 A - 1)}$$

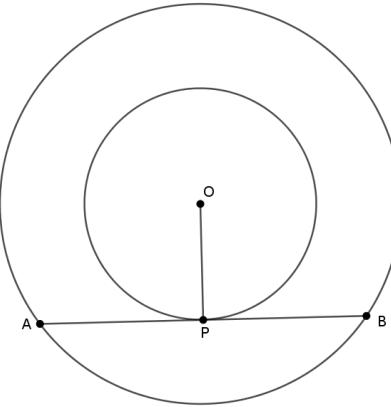
1

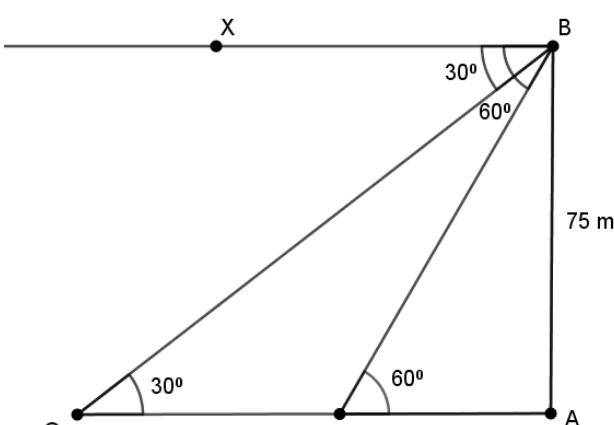
$$= \frac{\sin A [1 - 2(1 - \cos^2 A)]}{\cos A [2 \cos^2 A - 1]} = \frac{\sin A [1 - 2 + 2 \cos^2 A]}{\cos A [2 \cos^2 A - 1]}$$

1

$$= \frac{\sin A [2 \cos^2 A - 1]}{\cos A [2 \cos^2 A - 1]} = \tan A = \text{RHS}$$

1

OR	
29(B).	Prove that $\sec A (1 - \sin A) (\sec A + \tan A) = 1$.
Sol.	$\text{LHS} = \sec A (1 - \sin A) (\sec A + \tan A)$ $= \frac{1}{\cos A} (1 - \sin A) \left(\frac{1}{\cos A} + \frac{\sin A}{\cos A} \right) \quad 1$ $= \frac{1}{\cos A} (1 - \sin A) \frac{(1 + \sin A)}{\cos A} \quad 1$ $= \frac{1 - \sin^2 A}{\cos^2 A} = \frac{\cos^2 A}{\cos^2 A} = 1 = \text{RHS} \quad 1$
30.	Two concentric circles are of radii 5 cm and 3 cm. Find the length of the chord of the larger circle which touches the smaller circle.
Sol.	<p>AB is the chord of larger circle touching the smaller circle at P.</p>  <p>$OA = 5 \text{ cm}$, $OP = 3 \text{ cm}$</p> <p>To find AB</p> <p>$OP \perp AB$ (radius \perp tangent)</p> <p>AB is the chord of larger circle and $OP \perp AB$</p> <p>$\therefore AP = PB$</p> <p>In right-angled $\triangle AOP$, $AP^2 = 5^2 - 3^2 = 16$</p> <p>$AP = 4 \text{ cm}$</p>

	$\therefore AB = 2AP = 8 \text{ cm}$	$\frac{1}{2}$
31.	Find the value of 'p' for which the quadratic equation $px(x - 2) + 6 = 0$ has two equal real roots.	
Sol.	$px(x - 2) + 6 = 0 \Rightarrow px^2 - 2px + 6 = 0$ $a = p, b = -2p, c = 6$ <p>Quadratic equation has equal roots, $\therefore D = 0$</p> $b^2 - 4ac = 0 \Rightarrow 4p^2 - 24p = 0$ $4p(p - 6) = 0$ $p = 0, p = 6$ <p>$p = 0$ rejected $\therefore p = 6$</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
	SECTION D This section comprises of Long Answer (LA) type questions of 5 marks each.	
32(A).	A straight highway leads to the foot of a tower. A man standing on the top of the 75 m high tower observes two cars at angles of depression of 30° and 60° , which are approaching the foot of the tower. If one car is exactly behind the other on the same side of the tower, find the distance between the two cars. (use $\sqrt{3} = 1.73$)	
Sol.		1 mark for correct figure

AB = Height of tower = 75 m

P, Q are positions of cars

$$\angle XBQ = \angle BQA = 30^\circ$$

$$\angle XBP = \angle BPA = 60^\circ$$

$$\text{In } \Delta APB, \tan 60^\circ = \frac{75}{AP} \Rightarrow AP = \frac{75}{\sqrt{3}} = 25\sqrt{3}$$

$$\text{In } \Delta AQB, \tan 30^\circ = \frac{75}{AQ} \Rightarrow AQ = 75\sqrt{3}$$

$$\text{Distance between the cars} = PQ = AQ - AP$$

$$= 75\sqrt{3} - 25\sqrt{3} = 50\sqrt{3}$$

$$= 50 \times 1.73 = 86.5 \text{ m}$$

$1\frac{1}{2}$

$1\frac{1}{2}$

$\frac{1}{2}$

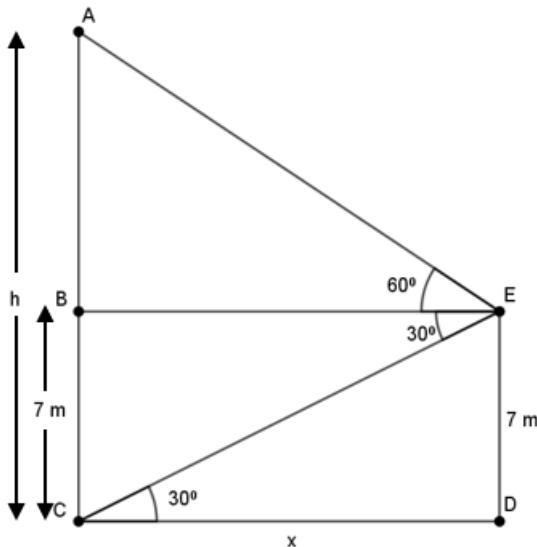
$\frac{1}{2}$

OR

32(B).

From the top of a 7 m high building, the angle of elevation of the top of a cable tower is 60° and the angle of depression of its foot is 30° . Determine the height of the tower.

Sol.



**1 mark
for
correct
figure**

Let AC be h m, $BC = DE = 7$ m, $AB = (h-7)$ m

$\angle AEB = 60^\circ$ and $\angle BEC = 30^\circ$

$\therefore \angle ECD = 30^\circ$

Let CD be x m

$$\frac{DE}{CD} = \frac{7}{x} = \tan 30^\circ \Rightarrow x = 7\sqrt{3}$$

$$\Rightarrow BE = 7\sqrt{3}$$

$$\text{Again } \frac{AB}{BE} = \tan 60^\circ$$

$$\Rightarrow \frac{h-7}{7\sqrt{3}} = \sqrt{3}$$

$$\Rightarrow h = 28$$

\therefore Height of tower = 28 m

$1\frac{1}{2}$

1

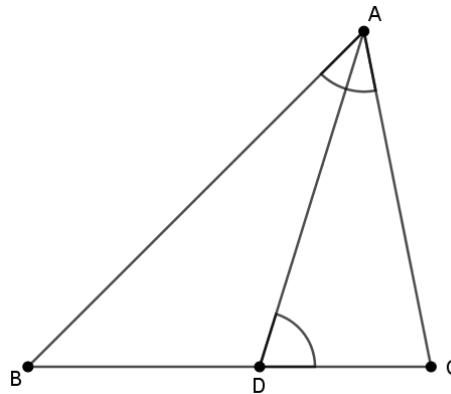
1

$\frac{1}{2}$

33(A).

D is a point on the side BC of a triangle ABC such that $\angle ADC = \angle BAC$, prove that $CA^2 = CB \cdot CD$

Sol.



**1 mark
for
correct
figure**

In $\triangle ABC$, D is a point on side BC such that $\angle ADC = \angle BAC$

In $\triangle CBA$ and $\triangle CDA$

$\angle C = \angle C$ (common)

$\angle BAC = \angle ADC$ (given)

$\therefore \triangle CBA \sim \triangle CAD$ (By AA similarity)

\therefore their corresponding sides are proportional

$$\Rightarrow \frac{CB}{CA} = \frac{CA}{CD} \Rightarrow CA^2 = CB \cdot CD$$

1

1

1

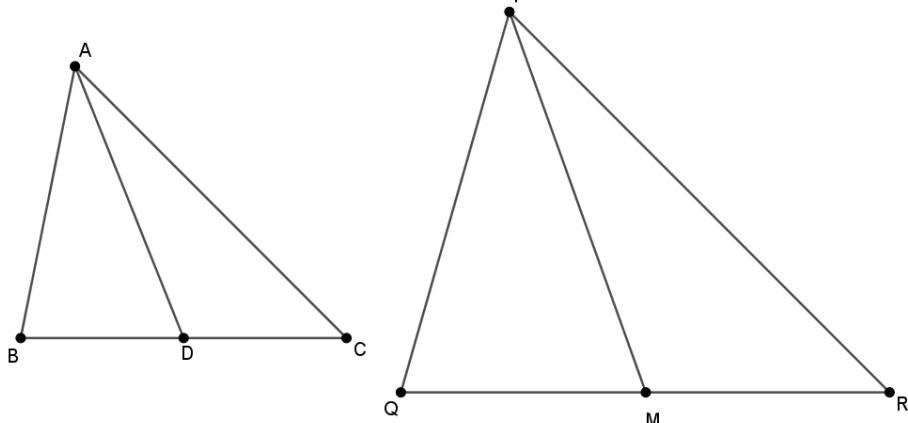
1

OR

33(B).

If AD and PM are medians of triangles ABC and PQR, respectively where $\triangle ABC \sim \triangle PQR$, prove that $\frac{AB}{PQ} = \frac{AD}{PM}$.

Sol.



**1 mark
for
correct
figure**

$$\triangle ABC \sim \triangle PQR$$

	<p>AD and AM are medians of $\triangle ABC$ and $\triangle PQR$ respectively.</p> <p>$\triangle ABC \sim \triangle PQR$</p> $\therefore \frac{AB}{PQ} = \frac{BC}{QR}$ $\frac{AB}{PQ} = \frac{2BD}{2QM}$ $\frac{AB}{PQ} = \frac{BD}{QM}$ <p>Also $\angle B = \angle Q$ ($\triangle ABC \sim \triangle PQR$)</p> <p>$\Rightarrow \triangle ABD \sim \triangle PQM$ (SAS similarly)</p> $\Rightarrow \frac{AB}{PQ} = \frac{AD}{PM}$	$1\frac{1}{2}$ $1\frac{1}{2}$ 1
34.	<p>A student was asked to make a model shaped like a cylinder with two cones attached to its ends by using a thin aluminium sheet. The diameter of the model is 3 cm and its total length is 12 cm. If each cone has a height of 2 cm, find the volume of air contained in the model.</p>	
Sol.	<p>Radius of each cone = Radius of cylinder = $\frac{3}{2}$ cm</p> <p>Height of each cone 'H' = 2 cm</p> <p>Height of cylinder 'h' = $12 - 4 = 8$ cm</p> <p>Volume of air = Volume of cylinder + Volume of 2 cones</p> $= \pi r^2 h + 2 \frac{1}{3} \pi r^2 H$ $= \pi r^2 \left(h + \frac{2}{3} H \right) = \frac{22}{7} \times \frac{3}{2} \times \frac{3}{2} \left(8 + \frac{2}{3} \times 2 \right)$ $= \frac{22}{7} \times \frac{9}{4} \times \frac{28}{3} = 66 \text{ cm}^3$	1 $1\frac{1}{2} + 1\frac{1}{2}$ 1

35.

The monthly expenditure on milk in 200 families of a Housing Society is given below :

Monthly Expenditure (in ₹)	1000-1500	1500-2000	2000-2500	2500-3000	3000-3500	3500-4000	4000-4500	4500-5000
Number of families	24	40	33	x	30	22	16	7

Find the value of x and also, find the median and mean expenditure on milk.

Sol.

Monthly Exp. (in ₹)	x	f_i	c_f	d	$x_i f_i$
1000 – 1500	1250	24	24	-3	-72
1500 – 2000	1750	40	64	-2	-80
2000 – 2500	2250	33	97	-1	-33
2500 – 3000	2750	$x=28$	125	0	0
3000 – 3500	3250	30	155	1	30
3500 – 4000	3750	22	177	2	44
4000 – 4500	4250	16	193	3	48
4500 – 5000	4750	7	200	4	28
Total					-35

$$172 + x = 200 \Rightarrow x = 28$$

l = lower limit of median class = 2500

$$\frac{N}{2} = \frac{200}{2} = 100$$

$$C = 97, f = 28, h = 500$$

2 for
correct
table

1

$$\begin{aligned}
 \text{Median} &= l + \frac{\frac{N}{2} - C}{f} \times h \\
 &= 2500 + \frac{100 - 97}{28} \times 500 \\
 &= 2500 + \frac{3}{28} \times 500 = 2553.6
 \end{aligned}$$

Median Expenditure = ₹ 2553.6

$$\text{Mean} = 2750 - \frac{35 \times 500}{200} = 2750 - 87.5 = 2662.5$$

Mean Expenditure = ₹ 2662.5

1

1

SECTION E
This section comprises of 3 case-study based questions of 4 marks each.

36.

Two schools 'P' and 'Q' decided to award prizes to their students for two games of Hockey ₹ x per student and Cricket ₹ y per student. School 'P' decided to award a total of ₹ 9,500 for the two games to 5 and 4 students respectively; while school 'Q' decided to award ₹ 7,370 for the two games to 4 and 3 students respectively.



Based on the above information, answer the following questions :

- Represent the following information algebraically (in terms of x and y).
- (a) What is the prize amount for hockey ?

OR

- (b) Prize amount on which game is more and by how much ?
- What will be the total prize amount if there are 2 students each from two games ?

Sol.

- $5x + 4y = 9500$ _____ (1)
- $4x + 3y = 7370$ _____ (2)

**1
2
1
2**

(ii) (a) Solving (1) and (2), $x = 980$

\therefore Prize Amount for Hockey = ₹ 980

OR

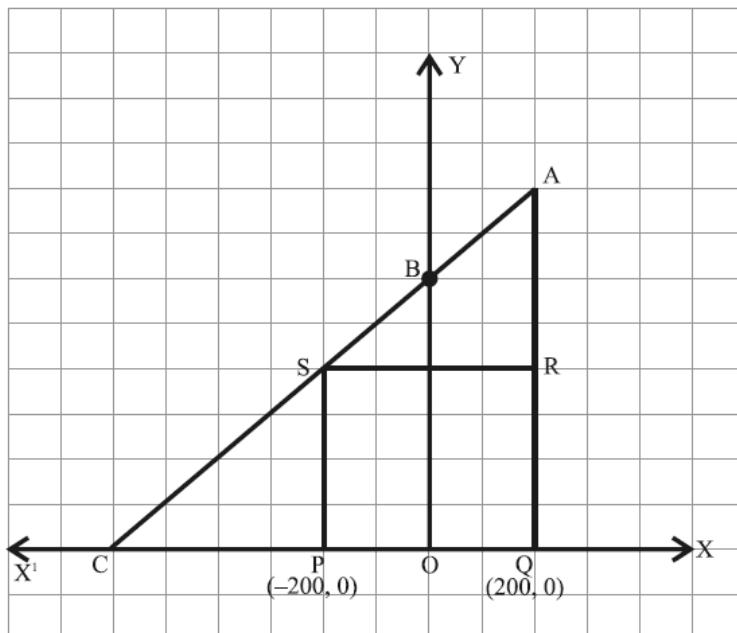
(ii) (b) On solving $x = 980$, $y = 1,150$

\therefore Prize Amount for Cricket is more by ₹ $(1,150 - 980) = ₹ 170$

(iii) $2(x + y) = 2(980 + 1150) = 2(2130) = ₹ 4,260$

37.

Jagdish has a field which is in the shape of a right angled triangle AQC. He wants to leave a space in the form of a square PQRS inside the field for growing wheat and the remaining for growing vegetables (as shown in the figure). In the field, there is a pole marked as O.



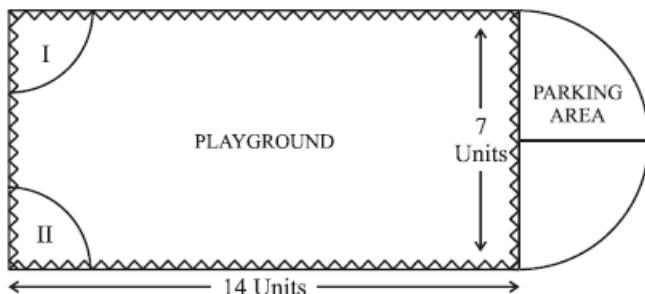
Based on the above information, answer the following questions :

(i) Taking O as origin, coordinates of P are $(-200, 0)$ and of Q are $(200, 0)$. PQRS being a square, what are the coordinates of R and S ?

	<p>(ii) (a) What is the area of square PQRS ?</p> <p style="text-align: center;">OR</p> <p>(b) What is the length of diagonal PR in square PQRS ?</p> <p>(iii) If S divides CA in the ratio K:1, what is the value of K, where point A is (200, 800) ?</p>	
Sol.	<p>(i) R(200, 400), S(-200, 400)</p> <p>(ii) (a) side PQ = (200+200) m = 400 m</p> <p>Area of square PQRS = 400×400</p> <p style="text-align: right;">= 160000 sq. units</p> <p style="text-align: center;">OR</p> <p>(ii) (b) Diagonal PR = $\sqrt{(400)^2 + (400)^2}$</p> <p style="text-align: right;">$= \sqrt{3200}$ or $400\sqrt{2}$</p> <p>(iii) C(-600,0); A(200,800); S(-200,400)</p> <p>S divides CA in the ratio $k:1$</p> $-200 = \frac{k(200)+1(-600)}{k+1}$ $\Rightarrow k = 1$	<p style="text-align: right;">$\frac{1}{2} + \frac{1}{2}$</p> <p style="text-align: right;">1</p>

38.

Governing council of a local public development authority of Dehradun decided to build an adventurous playground on the top of a hill, which will have adequate space for parking.



After survey, it was decided to build rectangular playground, with a semi-circular area allotted for parking at one end of the playground. The length and breadth of the rectangular playground are 14 units and 7 units, respectively. There are two quadrants of radius 2 units on one side for special seats.

Based on the above information, answer the following questions :

- What is the total perimeter of the parking area ?
- (a) What is the total area of parking and the two quadrants ?

OR

- What is the ratio of area of playground to the area of parking area ?
- Find the cost of fencing the playground and parking area at the rate of ₹ 2 per unit.

Sol.

(i) Total perimeter = $\pi r + 2r$

$$= \frac{22}{7} \times \frac{7}{2} + 7 = 18 \text{ units}$$

1

(ii) (a) Area of parking = $\frac{1}{2} \pi r^2 = \frac{1}{2} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} = \frac{77}{4}$

1

$$\text{Area of quadrants} = 2 \cdot \frac{22}{7} \times 2 \times 2 \times \frac{1}{4} = \frac{44}{7}$$

1
2

$$\text{Total Area} = \frac{77}{4} + \frac{44}{7} = \frac{715}{28} \text{ or } 25.54 \text{ sq. units}$$

1
2

OR

$$(ii) (b) \frac{\text{Area of playground}}{\text{Area of parking}} = \frac{98}{77/4} = \frac{56}{11} = 56 : 11$$

1+1

$$(iii) \text{Required Perimeter} = 2(l + b) + \frac{2\pi r}{2}$$
$$= 2(14 + 7) + \frac{22}{7} \times \frac{7}{2} = 53 \text{ units}$$

**1
2**

$$\text{Cost of fencing} = 53 \times 2 = \text{₹} 106$$

**1
2**