



Series WX1YZ/6



SET~3

रोल नं. Roll No.						
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प्रश्न-पत्र कोड
Q.P. Code **30/6/3**

परीक्षार्थी प्रश्न-पत्र कोड को उत्तर-पुस्तिका के मुख-पृष्ठ पर अवश्य लिखें।

Candidates must write the Q.P. Code on the title page of the answer-book.

गणित (मानक) – सैद्धान्तिक

MATHEMATICS (Standard) – Theory

निर्धारित समय : 3 घण्टे

Time allowed : 3 hours

अधिकतम अंक : 80

Maximum Marks : 80

नोट / NOTE :

- (i) कृपया जाँच कर लें कि इस प्रश्न-पत्र में मुद्रित पृष्ठ 23 हैं।
Please check that this question paper contains 23 printed pages.
- (ii) प्रश्न-पत्र में दाहिने हाथ की ओर दिए गए प्रश्न-पत्र कोड को परीक्षार्थी उत्तर-पुस्तिका के मुख-पृष्ठ पर लिखें।
Q.P. Code given on the right hand side of the question paper should be written on the title page of the answer-book by the candidate.
- (iii) कृपया जाँच कर लें कि इस प्रश्न-पत्र में 38 प्रश्न हैं।
Please check that this question paper contains 38 questions.
- (iv) कृपया प्रश्न का उत्तर लिखना शुरू करने से पहले, उत्तर-पुस्तिका में प्रश्न का क्रमांक अवश्य लिखें।
Please write down the serial number of the question in the answer-book before attempting it.
- (v) इस प्रश्न-पत्र को पढ़ने के लिए 15 मिनट का समय दिया गया है। प्रश्न-पत्र का वितरण पूर्वाह्न में 10.15 बजे किया जाएगा। 10.15 बजे से 10.30 बजे तक परीक्षार्थी केवल प्रश्न-पत्र को पढ़ेंगे और इस अवधि के दौरान वे उत्तर-पुस्तिका पर कोई उत्तर नहीं लिखेंगे।
15 minute time has been allotted to read this question paper. The question paper will be distributed at 10.15 a.m. From 10.15 a.m. to 10.30 a.m., the candidates will read the question paper only and will not write any answer on the answer-book during this period.





General Instructions :

Read the following instructions carefully and follow them :

- (i) This question paper contains **38** questions. All questions are compulsory.
- (ii) This Question Paper is divided into **FIVE** Sections – **Section A, B, C, D and E**.
- (iii) In Section–A question number **1** to **18** are Multiple Choice Questions (MCQs) and question number **19 & 20** are Assertion-Reason based questions of **1** mark each.
- (iv) In Section–B question number **21** to **25** are Very Short-Answer-I (SA-I) type questions of **2** marks each.
- (v) In Section–C question number **26** to **31** are Short Answer-II (SA-II) type questions carrying **3** marks each.
- (vi) In Section–D question number **32** to **35** are Long Answer (LA) type questions carrying **5** marks each.
- (vii) In Section–E question number **36** to **38** are Case Study / Passage based integrated units of assessment questions carrying **4** marks each. Internal choice is provided in **2** marks question in each case-study.
- (viii) There is no overall choice. However, an internal choice has been provided in **2** questions in Section–B, **2** questions in Section–C, **2** questions in Section–D and **3** question in Section–E.
- (ix) Draw neat figures wherever required. Take $\pi = \frac{22}{7}$ wherever required if not stated.
- (x) Use of calculator is NOT allowed.

SECTION – A (Multiple Choice Questions)

Section – A consists of 20 questions of 1 mark each.

1. The distance between the points (0, 5) and (-3, 1) is :
 - (A) 8 units
 - (B) 5 units
 - (C) 3 units
 - (D) 25 units



2. If $\tan \theta = \frac{x}{y}$, then $\cos \theta$ is equal to

(A) $\frac{x}{\sqrt{x^2 + y^2}}$ (B) $\frac{y}{\sqrt{x^2 + y^2}}$
(C) $\frac{x}{\sqrt{x^2 - y^2}}$ (D) $\frac{y}{\sqrt{x^2 - y^2}}$

3. The zeroes of the polynomial $3x^2 + 11x - 4$ are :

(A) $\frac{1}{3}, -4$ (B) $-\frac{1}{3}, 4$
(C) $\frac{1}{3}, 4$ (D) $-\frac{1}{3}, -4$

4. The circumferences of two circles are in the ratio $4 : 5$. What is the ratio of their radii ?

(A) $16 : 25$ (B) $25 : 16$
(C) $2 : \sqrt{5}$ (D) $4 : 5$

5. If the sum of the first n terms of an A.P be $3n^2 + n$ and its common difference is 6, then its first term is

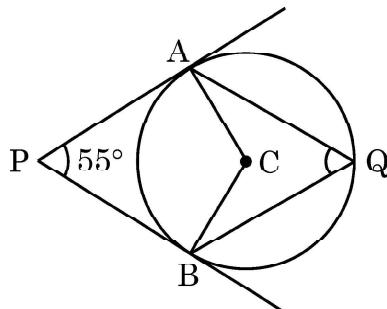
(A) 2 (B) 3
(C) 1 (D) 4

6. If the zeroes of the quadratic polynomial $x^2 + (a + 1)x + b$ are 2 and -3 , then

(A) $a = -7, b = -1$ (B) $a = 5, b = -1$
(C) $a = 2, b = -6$ (D) $a = 0, b = -6$

7. If $p^2 = \frac{32}{50}$, then p is a/an

(A) whole number (B) integer
(C) rational number (D) irrational number



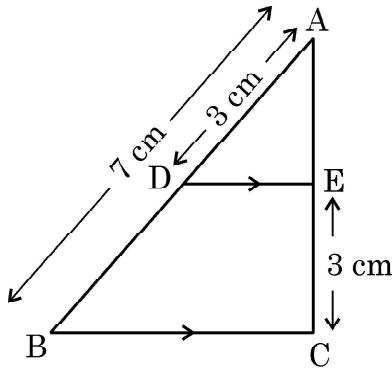
(A) $62\frac{1}{2}^\circ$ (B) 125°
(C) 55° (D) 90°

11. If α and β are the zeroes of the polynomial $x^2 - 1$, then the value of $(\alpha + \beta)$ is
(A) 2 (B) 1
(C) -1 (D) 0

12. If $\triangle PQR \sim \triangle ABC$; $PQ = 6$ cm, $AB = 8$ cm and the perimeter of $\triangle ABC$ is 36 cm, then the perimeter of $\triangle PQR$ is
(A) 20.25 cm (B) 27 cm
(C) 48 cm (D) 64 cm



13. In the given figure, $DE \parallel BC$. If $AD = 3 \text{ cm}$, $AB = 7 \text{ cm}$ and $EC = 3 \text{ cm}$, then the length of AE is



(A) 2 cm (B) 2.25 cm
(C) 3.5 cm (D) 4 cm

14. The volume of a right circular cone whose area of the base is 156 cm^2 and the vertical height is 8 cm, is
(A) 2496 cm^3 (B) 1248 cm^3
(C) 1664 cm^3 (D) 416 cm^3

15. A card is drawn at random from a well shuffled deck of 52 playing cards. The probability of getting a face card is
(A) $\frac{1}{2}$ (B) $\frac{3}{13}$
(C) $\frac{4}{13}$ (D) $\frac{1}{13}$

16. If 'p' is a root of the quadratic equation $x^2 - (p + q)x + k = 0$, then the value of 'k' is
(A) p (B) q
(C) $p + q$ (D) pq



Assertion – Reason Based Questions : In question numbers 19 and 20, a statement of Assertion (A) is followed by a statement of Reason (R). Choose the correct option out of the following :

(A) Both Assertion (A) and Reason (R) are true; and Reason (R) is the correct explanation of Assertion (A).

(B) Both Assertion (A) and Reason (R) are true; but Reason (R) is not the correct explanation of Assertion (A).

(C) Assertion (A) is true but Reason (R) is false.

(D) Assertion (A) is false but Reason (R) is true.

19. **Statement A (Assertion) :** For $0 < \theta \leq 90^\circ$, $\operatorname{cosec} \theta - \cot \theta$ and $\operatorname{cosec} \theta + \cot \theta$ are reciprocal of each other.

Statement R (Reason) : $\csc^2 \theta - \cot^2 \theta = 1$

20. **Statement A (Assertion) :** If $5 + \sqrt{7}$ is a root of a quadratic equation with rational co-efficients, then its other root is $5 - \sqrt{7}$.

Statement R (Reason) : Surd roots of a quadratic equation with rational co-efficients occur in conjugate pairs.

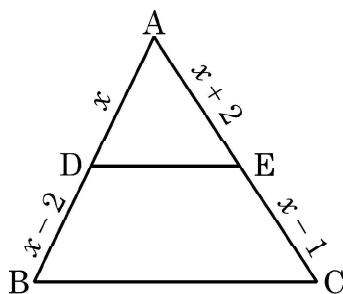


SECTION - B

Section – B consists of Very Short Answer (VSA) type of questions of **2** marks each.

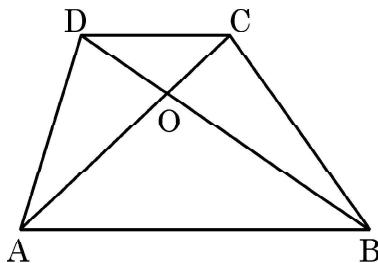
21. Find the ratio in which the y-axis divides the line segment joining the points $(5, - 6)$ and $(-1, - 4)$.

22. (A) In the given figure, ABC is a triangle in which $DE \parallel BC$. If $AD = x$, $DB = x - 2$, $AE = x + 2$ and $EC = x - 1$, then find the value of x .



OR

(B) Diagonals AC and BD of trapezium $ABCD$ with $AB \parallel DC$ intersect each other at point O . Show that $\frac{OA}{OC} = \frac{OB}{OD}$.



23. (A) Show that 6^n can not end with digit 0 for any natural number 'n'.

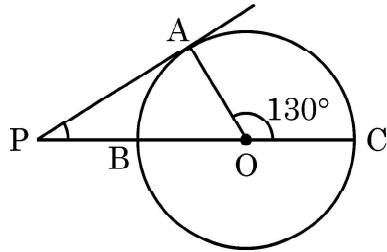
OR

(B) Find the LCM and HCF of 72 and 120

24. Find the length of the shadow on the ground of a pole of height 18 m when angle of elevation θ of the sun is such that $\tan \theta = \frac{6}{7}$.



25. In the given figure, PA is a tangent to the circle drawn from the external point P and PBC is the secant to the circle with BC as diameter. If $\angle AOC = 130^\circ$, then find the measure of $\angle APB$, where O is the centre of the circle.



SECTION - C

Section - C consists of Short Answer (SA) type of questions of 3 marks each.

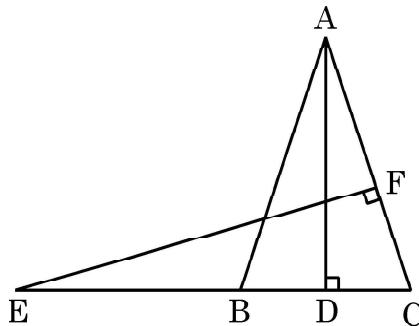
26. Prove that $(\sin \theta + \cos \theta)(\tan \theta + \cot \theta) = \sec \theta + \operatorname{cosec} \theta$.

27. (A) A natural number, when increased by 12, equals 160 times its reciprocal. Find the number.
OR
(B) If one root of the quadratic equation $x^2 + 12x - k = 0$ is thrice the other root, then find the value of k.

28. Find the ratio in which the line segment joining the points A(6, 3) and B(-2, -5) is divided by x-axis.

29. In a circle of radius 21 cm, an arc subtends an angle of 60° at the centre. Find the area of the sector formed by the arc. Also, find the length of the arc.

30. In the given figure, E is a point on the side CB produced of an isosceles triangle ABC with $AB = AC$. If $AD \perp BC$ and $EF \perp AC$, then prove that $\triangle ABD \sim \triangle ECF$.





31. (A) Find the HCF and LCM of 26, 65 and 117, using prime factorisation.

OR

(B) Prove that $\sqrt{2}$ is an irrational number.

SECTION – D

Section – D consists of Long Answer (LA) type questions of **5** marks each.

32. (A) The sum of first seven terms of an A.P. is 182. If its 4th term and the 17th term are in the ratio 1 : 5, find the A.P.

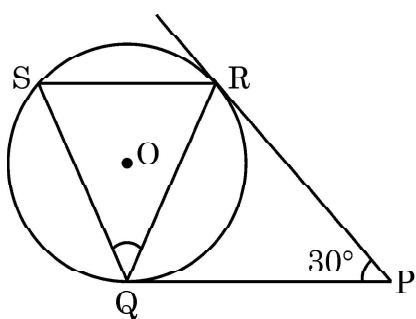
OR

(B) The sum of first q terms of an A.P. is $63q - 3q^2$. If its p^{th} term is -60 , find the value of p . Also, find the 11th term of this A.P.

33. (A) Prove that a parallelogram circumscribing a circle is a rhombus.

OR

(B)



In the given figure, tangents PQ and PR are drawn to a circle such that $\angle RPQ = 30^\circ$. A chord RS is drawn parallel to the tangent PQ . Find the measure of $\angle RQS$.



34. 250 apples of a box were weighed and the distribution of masses of the apples is given in the following table :

Mass (in grams)	80 – 100	100 – 120	120 – 140	140 – 160	160 – 180
Number of apples	20	60	70	x	60

(i) Find the value of x and the mean mass of the apples. 3

(ii) Find the modal mass of the apples 2

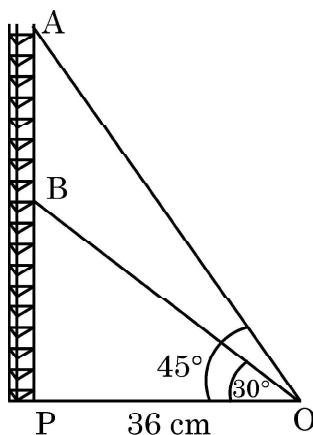
35. A solid is in the shape of a right-circular cone surmounted on a hemisphere, the radius of each of them being 7 cm and the height of the cone is equal to its diameter. Find the volume of the solid.

SECTION – E

3 Case Study Based Questions. Each question is of **4** marks.

36. Radio towers are used for transmitting a range of communication services including radio and television. The tower will either act as an antenna itself or support one or more antennas on its structure. On a similar concept, a radio station tower was built in two Sections A and B. Tower is supported by wires from a point O.

Distance between the base of the tower and point O is 36 cm. From point O, the angle of elevation of the top of the Section B is 30° and the angle of elevation of the top of Section A is 45° .





Based on the above information, answer the following questions :

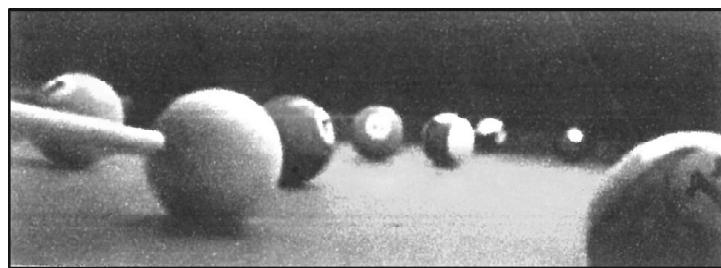
(i) Find the length of the wire from the point O to the top of Section B. 1
(ii) Find the distance AB. 2

OR

Find the area of ΔOPB .

(iii) Find the height of the Section A from the base of the tower. 1

37. "Eight Ball" is a game played on a pool table with 15 balls numbered 1 to 15 and a "cue ball" that is solid and white. Of the 15 numbered balls, eight are solid (non-white) coloured and numbered 1 to 8 and seven are striped balls numbered 9 to 15.



The 15 numbered pool balls (no cue ball) are placed in a large bowl and mixed, then one ball is drawn out at random.

Based on the above information, answer the following questions :

(i) What is the probability that the drawn ball bears number 8 ?
(ii) What is the probability that the drawn ball bears an even number ?

OR

What is the probability that the drawn ball bears a number, which is a multiple of 3 ?

(iii) What is the probability that the drawn ball is a solid coloured and bears an even number ?



38. A coaching institute of Mathematics conducts classes in two batches I and II and fees for rich and poor children are different. In batch I, there are 20 poor and 5 rich children, whereas in batch II, there are 5 poor and 25 rich children. The total monthly collection of fees from batch I is ₹ 9000 and from batch II is ₹ 26,000. Assume that each poor child pays ₹ x per month and each rich child pays ₹ y per month.



Based on the above information, answer the following questions :

(i) Represent the information given above in terms of x and y . 1
(ii) Find the monthly fee paid by a poor child. 2

OR

Find the difference in the monthly fee paid by a poor child and a rich child.

(iii) If there are 10 poor and 20 rich children in batch II, what is the total monthly collection of fees from batch II ? 1

Marking Scheme
Strictly Confidential
(For Internal and Restricted use only)
Secondary School Examination, 2023
MATHEMATICS PAPER CODE 30/6/3

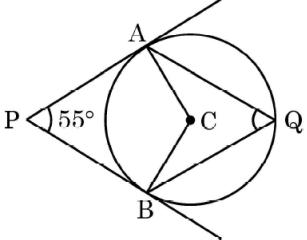
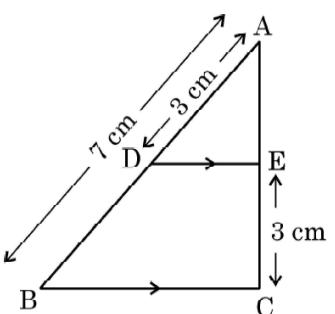
General Instructions: -

1	You are aware that evaluation is the most important process in the actual and correct assessment of the candidates. A small mistake in evaluation may lead to serious problems which may affect the future of the candidates, education system and teaching profession. To avoid mistakes, it is requested that before starting evaluation, you must read and understand the spot evaluation guidelines carefully.
2	“Evaluation policy is a confidential policy as it is related to the confidentiality of the examinations conducted, Evaluation done and several other aspects. Its’ leakage to public in any manner could lead to derailment of the examination system and affect the life and future of millions of candidates. Sharing this policy/document to anyone, publishing in any magazine and printing in News Paper/Website etc may invite action under various rules of the Board and IPC.”
3	Evaluation is to be done as per instructions provided in the Marking Scheme. It should not be done according to one’s own interpretation or any other consideration. Marking Scheme should be strictly adhered to and religiously followed. However, while evaluating, answers which are based on latest information or knowledge and/or are innovative, they may be assessed for their correctness otherwise and due marks be awarded to them.
4	The Marking scheme carries only suggested value points for the answers. These are in the nature of Guidelines only and do not constitute the complete answer. The students can have their own expression and if the expression is correct, the due marks should be awarded accordingly.
5	The Head-Examiner must go through the first five answer books evaluated by each evaluator on the first day, to ensure that evaluation has been carried out as per the instructions given in the Marking Scheme. If there is any variation, the same should be zero after deliberation and discussion. The remaining answer books meant for evaluation shall be given only after ensuring that there is no significant variation in the marking of individual evaluators.
6	Evaluators will mark (✓) wherever answer is correct. For wrong answer CROSS ‘X’ be marked. Evaluators will not put right (✓) while evaluating which gives an impression that answer is correct and no marks are awarded. This is most common mistake which evaluators are committing.
7	If a question has parts, please award marks on the right-hand side for each part. Marks awarded for different parts of the question should then be totaled up and written in the left-hand margin and encircled. This may be followed strictly.
8	If a question does not have any parts, marks must be awarded in the left-hand margin and encircled. This may also be followed strictly.

9	<u>In Q1-Q20, if a candidate attempts the question more than once (without canceling the previous attempt), marks shall be awarded for the first attempt only and the other answer scored out with a note “Extra Question”.</u>
10	<u>In Q21-Q38, if a student has attempted an extra question, answer of the question deserving more marks should be retained and the other answer scored out with a note “Extra Question”.</u>
11	No marks to be deducted for the cumulative effect of an error. It should be penalized only once.
12	A full scale of marks _____(example 0 to 80/70/60/50/40/30 marks as given in Question Paper) has to be used. Please do not hesitate to award full marks if the answer deserves it.
13	Every examiner has to necessarily do evaluation work for full working hours i.e., 8 hours every day and evaluate 20 answer books per day in main subjects and 25 answer books per day in other subjects (Details are given in Spot Guidelines). This is in view of the reduced syllabus and number of questions in question paper.
14	Ensure that you do not make the following common types of errors committed by the Examiner in the past:- <ul style="list-style-type: none"> ● Leaving answer or part thereof unassessed in an answer book. ● Giving more marks for an answer than assigned to it. ● Wrong totaling of marks awarded on an answer. ● Wrong transfer of marks from the inside pages of the answer book to the title page. ● Wrong question wise totaling on the title page. ● Wrong totaling of marks of the two columns on the title page. ● Wrong grand total. ● Marks in words and figures not tallying/not same. ● Wrong transfer of marks from the answer book to online award list. ● Answers marked as correct, but marks not awarded. (Ensure that the right tick mark is correctly and clearly indicated. It should merely be a line. Same is with the X for incorrect answer.) ● Half or a part of answer marked correct and the rest as wrong, but no marks awarded.
15	While evaluating the answer books if the answer is found to be totally incorrect, it should be marked as cross (X) and awarded zero (0)Marks.
16	Any un assessed portion, non-carrying over of marks to the title page, or totaling error detected by the candidate shall damage the prestige of all the personnel engaged in the evaluation work as also of the Board. Hence, in order to uphold the prestige of all concerned, it is again reiterated that the instructions be followed meticulously and judiciously.
17	The Examiners should acquaint themselves with the guidelines given in the “ Guidelines for spot Evaluation ” before starting the actual evaluation.
18	Every Examiner shall also ensure that all the answers are evaluated, marks carried over to the title page, correctly totaled and written in figures and words.
19	The candidates are entitled to obtain photocopy of the Answer Book on request on payment of the prescribed processing fee. All Examiners/Additional Head Examiners/Head Examiners are once again reminded that they must ensure that evaluation is carried out strictly as per value points for each answer as given in the Marking Scheme.

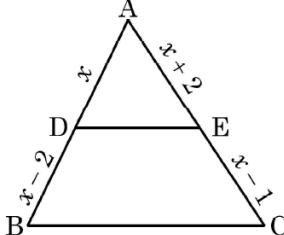
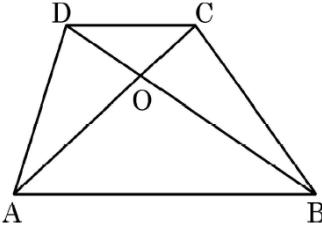
MARKING SCHEME
MATHEMATICS (Subject Code-041)
(PAPER CODE: 30/6/3)

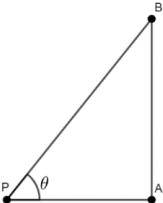
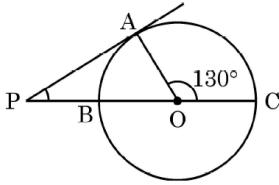
5.	If the sum of the first n terms of an A.P be $3n^2 + n$ and its common difference is 6, then its first term is (A) 2 (B) 3 (C) 1 (D) 4	
Sol.	(D) 4	1
6.	If the zeroes of the quadratic polynomial $x^2 + (a + 1)x + b$ are 2 and -3, then (A) $a = -7, b = -1$ (B) $a = 5, b = -1$ (C) $a = 2, b = -6$ (D) $a = 0, b = -6$	
Sol.	(D) $a = 0, b = -6$	1
7.	If $p^2 = \frac{32}{50}$, then p is a/an (A) whole number (B) integer (C) rational number (D) irrational number	
Sol.	(C) rational	1
8.	If θ is an acute angle of a right angled triangle, then which of the following equation is not true ? (A) $\sin \theta \cot \theta = \cos \theta$ (B) $\cos \theta \tan \theta = \sin \theta$ (C) $\operatorname{cosec}^2 \theta - \cot^2 \theta = 1$ (D) $\tan^2 \theta - \sec^2 \theta = 1$	
Sol.	(D) $\tan^2 \theta - \sec^2 \theta = 1$	1
9.	The point of intersection of the line represented by $3x - y = 3$ and the y-axis is given by (A) $(0, -3)$ (B) $(0, 3)$ (C) $(2, 0)$ (D) $(-2, 0)$	
Sol.	(A) $(0, -3)$	1

10.	<p>In the given figure, PA and PB are tangents from external point P to a circle with centre C and Q is any point on the circle. Then the measure of $\angle AQB$ is</p>  <p>(A) $62\frac{1}{2}^\circ$ (B) 125° (C) 55° (D) 90°</p>	
Sol.	(A) $62\frac{1}{2}^\circ$	1
11.	<p>If α and β are the zeroes of the polynomial $x^2 - 1$, then the value of $(\alpha + \beta)$ is</p> <p>(A) 2 (B) 1 (C) -1 (D) 0</p>	
Sol.	(D) 0	1
12.	<p>If $\triangle PQR \sim \triangle ABC$; $PQ = 6$ cm, $AB = 8$ cm and the perimeter of $\triangle ABC$ is 36 cm, then the perimeter of $\triangle PQR$ is</p> <p>(A) 20.25 cm (B) 27 cm (C) 48 cm (D) 64 cm</p>	
Sol.	(B) 27 cm	1
13.	<p>In the given figure, $DE \parallel BC$. If $AD = 3$ cm, $AB = 7$ cm and $EC = 3$ cm, then the length of AE is</p>  <p>(A) 2 cm (B) 2.25 cm (C) 3.5 cm (D) 4 cm</p>	
Sol.	(B) 2.25 cm	1

14.	<p>The volume of a right circular cone whose area of the base is 156 cm^2 and the vertical height is 8 cm, is</p> <p>(A) 2496 cm^3 (B) 1248 cm^3 (C) 1664 cm^3 (D) 416 cm^3</p>	
Sol.	(D) 416 cm^3	1
15.	<p>A card is drawn at random from a well shuffled deck of 52 playing cards. The probability of getting a face card is</p> <p>(A) $\frac{1}{2}$ (B) $\frac{3}{13}$ (C) $\frac{4}{13}$ (D) $\frac{1}{13}$</p>	
Sol.	(B) $\frac{3}{13}$	1
16.	<p>If 'p' is a root of the quadratic equation $x^2 - (p + q)x + k = 0$, then the value of 'k' is</p> <p>(A) p (B) q (C) $p + q$ (D) pq</p>	
Sol.	(D) pq	1
17.	<p>Cards bearing numbers 3 to 20 are placed in a bag and mixed thoroughly. A card is taken out of the bag at random. What is the probability that the number on the card taken out is an even number ?</p> <p>(A) $\frac{9}{17}$ (B) $\frac{1}{2}$ (C) $\frac{5}{9}$ (D) $\frac{7}{18}$</p>	
Sol.	(B) $\frac{1}{2}$	1
18.	<p>The condition for the system of linear equations $ax + by = c$; $lx + my = n$ to have a unique solution is</p> <p>(A) $am \neq bl$ (B) $al \neq bm$ (C) $al = bm$ (D) $am = bl$</p>	
Sol.	(A) $am \neq bl$	1

	<p>Assertion – Reason Based Questions : In question numbers 19 and 20, a statement of Assertion (A) is followed by a statement of Reason (R). Choose the correct option out of the following :</p> <p>(A) Both Assertion (A) and Reason (R) are true; and Reason (R) is the correct explanation of Assertion (A).</p> <p>(B) Both Assertion (A) and Reason (R) are true; but Reason (R) is not the correct explanation of Assertion (A).</p> <p>(C) Assertion (A) is true but Reason (R) is false.</p> <p>(D) Assertion (A) is false but Reason (R) is true.</p>	
19.	<p>Statement A (Assertion) : For $0 < \theta \leq 90^\circ$, $\operatorname{cosec} \theta - \cot \theta$ and $\operatorname{cosec} \theta + \cot \theta$ are reciprocal of each other.</p> <p>Statement R (Reason) : $\operatorname{cosec}^2 \theta - \cot^2 \theta = 1$</p>	
Sol.	(A)	1
20.	<p>Statement A (Assertion) : If $5 + \sqrt{7}$ is a root of a quadratic equation with rational co-efficients, then its other root is $5 - \sqrt{7}$.</p> <p>Statement R (Reason) : Surd roots of a quadratic equation with rational co-efficients occur in conjugate pairs.</p>	
Sol.	(A)	1
	<p style="text-align: center;">SECTION – B</p> <p>Section – B consists of Very Short Answer (VSA) type of questions of 2 marks each.</p>	
21.	Find the ratio in which the y-axis divides the line segment joining the points $(5, -6)$ and $(-1, -4)$.	
Sol.	<p style="text-align: center;">$k : 1$</p> <p style="text-align: center;"></p> <p>Let $P(0, y)$ be the point on y axis which divides AB in the ratio $k : 1$</p>	
	$\frac{-k + 5}{k + 1} = 0 \Rightarrow k = 5$	$\frac{1}{2}$

	Ratio is 5 : 1	$\frac{1}{2}$
22(A).	In the given figure, ABC is a triangle in which $DE \parallel BC$. If $AD = x$, $DB = x - 2$, $AE = x + 2$ and $EC = x - 1$, then find the value of x .	
		
Sol.	<p>In $\triangle ABC$, $DE \parallel BC$</p> $\frac{AD}{DB} = \frac{AE}{EC} \Rightarrow \frac{x}{x-2} = \frac{x+2}{x-1}$ $x(x-1) = (x+2)(x-2)$ $x^2 - x = x^2 - 4 \Rightarrow x = 4$	1 1
	OR	
22(B).	Diagonals AC and BD of trapezium ABCD with $AB \parallel DC$ intersect each other at point O. Show that $\frac{OA}{OC} = \frac{OB}{OD}$.	
		
Sol.	<p>In $\triangle AOB$ and $\triangle COD$,</p> $\angle OAB = \angle OCD$ $\angle OBA = \angle ODC$ <p>Therefore, $\triangle AOB \sim \triangle COD$</p> $\therefore \frac{OA}{OC} = \frac{OB}{OD}$	$1\frac{1}{2}$ $\frac{1}{2}$

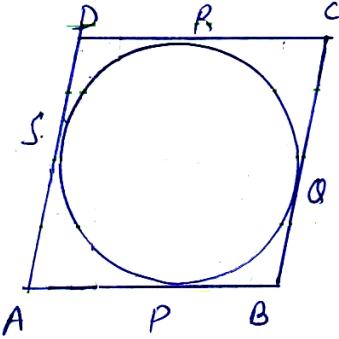
23(A).	Show that 6^n can not end with digit 0 for any natural number 'n'.	
Sol.	If 6^n ends with digit 0, it would be divisible by 5. So, prime factorization of 6^n would contain 5. But $6^n = (2 \times 3)^n$, the only prime factorization of 6^n are 2 and 3 as per fundamental theorem of Arithmetic . There is no other prime in the factorization of 6^n . So, there is no natural number n for which 6^n ends with digit zero.	2
	OR	
23(B).	Find the LCM and HCF of 72 and 120	
Sol.	$72 = 2^3 \times 3^2$ $120 = 2^3 \times 3 \times 5$ HCF = 24 LCM = 360	1 1
24.	Find the length of the shadow on the ground of a pole of height 18 m when angle of elevation θ of the sun is such that $\tan \theta = \frac{6}{7}$.	
Sol.	<p>Pole of height AB = 18 m AP = length of shadow In ΔAPB, $\tan \theta = \frac{18}{AP}$ $\frac{6}{7} = \frac{18}{AP}$ $\Rightarrow AP = 21$ m</p> 	1 1 2 1 2
25.	In the given figure, PA is a tangent to the circle drawn from the external point P and PBC is the secant to the circle with BC as diameter. If $\angle AOC = 130^\circ$, then find the measure of $\angle APB$, where O is the centre of the circle.	
		

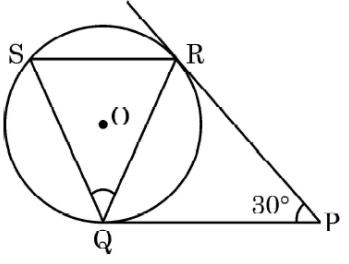
Sol.	$\angle AOB = 180^\circ - 30^\circ = 50^\circ$ $\angle OAP = 90^\circ$ $\therefore \angle APB = 180^\circ - (50^\circ + 90^\circ) = 40^\circ$	$\frac{1}{2}$ $\frac{1}{2}$ 1
	<p style="text-align: center;">SECTION C</p> <p>This section comprises of Short Answer (SA) type questions of 3 marks each.</p>	
26.	Prove that $(\sin \theta + \cos \theta)(\tan \theta + \cot \theta) = \sec \theta + \operatorname{cosec} \theta$.	
Sol.	$\begin{aligned} \text{LHS} &= (\sin \theta + \cos \theta) \left(\frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta} \right) \\ &= (\sin \theta + \cos \theta) \left(\frac{\sin^2 \theta + \cos^2 \theta}{\cos \theta \sin \theta} \right) \\ &= \frac{(\sin \theta + \cos \theta) \cdot (1)}{\cos \theta \sin \theta} \\ &= \sec \theta + \operatorname{cosec} \theta = \text{RHS} \end{aligned}$	1 1 $\frac{1}{2}$ $\frac{1}{2}$
27(A).	A natural number, when increased by 12, equals 160 times its reciprocal. Find the number.	
Sol.	<p>Let the natural number be x</p> $\text{ATQ, } x + 12 = \frac{160}{x}$ $x^2 + 12x = 160$ $x^2 + 12x - 160 = 0$ $(x + 20)(x - 8) = 0$ $x \neq -20, x = 8$	1 1 1 1

	\Rightarrow Required natural number is 8	
	OR	
27(B).	If one root of the quadratic equation $x^2 + 12x - k = 0$ is thrice the other root, then find the value of k.	
Sol.	$x^2 + 12x - k = 0$ <p>Let the roots be $\alpha, 3\alpha$</p> $\alpha + 3\alpha = -12 \Rightarrow \alpha = -3$ $\alpha \cdot 3\alpha = -k \Rightarrow 3\alpha^2 = -k$ $\Rightarrow k = -27$	$\frac{1}{2}$ 1 1 $\frac{1}{2}$
28.	Find the ratio in which the line segment joining the points A(6, 3) and B(-2, -5) is divided by x-axis.	
Sol.	<p>Let P(x, 0) be the point on x axis which divides AB in the ratio $k : 1$</p> $\frac{-5k + 3}{k + 1} = 0 \Rightarrow k = \frac{3}{5}$ <p>Ratio is 3 : 5</p>	$A(6, 3)$ $\frac{k : 1}{\bullet}$ $B(-2, -5)$ P $\frac{1}{2}$ 2 $\frac{1}{2}$
29.	In a circle of radius 21 cm, an arc subtends an angle of 60° at the centre. Find the area of the sector formed by the arc. Also, find the length of the arc.	
Sol.	$A = \frac{60}{360} \times \frac{22}{7} \times 21 \times 21 = 231 \text{ cm}^2$ $\text{Length of arc} = \frac{60}{360} \times 2 \times \frac{22}{7} \times 21 = 22 \text{ cm}$	$1\frac{1}{2}$ $1\frac{1}{2}$

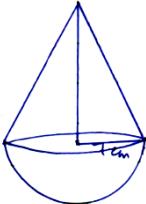
30.	<p>In the given figure, E is a point on the side CB produced of an isosceles triangle ABC with $AB = AC$. If $AD \perp BC$ and $EF \perp AC$, then prove that $\triangle ABD \sim \triangle ECF$.</p>	
Sol.	<p>Given ABC is an isosceles triangle, $\therefore AB = AC \Rightarrow \angle B = \angle C$</p> <p>In $\triangle ABD$ and $\triangle ECF$,</p> <p>$\angle ADB = \angle EFC$ (90° each, given)</p> <p>$\angle ABD = \angle ECF$</p> <p>$\therefore \triangle ABD \sim \triangle ECF$</p>	1 1 1 1
31(A).	Find the HCF and LCM of 26, 65 and 117, using prime factorisation.	
Sol.	$26 = 13 \times 2$ $65 = 13 \times 5$ $117 = 13 \times 3 \times 3$ $\therefore \text{HCF} = 13$ $\text{LCM} = 13 \times 2 \times 3 \times 5 \times 3 = 1170$	1 1 1
	OR	
31(B).	Prove that $\sqrt{2}$ is an irrational number.	
Sol.	<p>Let $\sqrt{2}$ be a rational number.</p> <p>$\therefore \sqrt{2} = \frac{p}{q}$, where $q \neq 0$ and let p & q be co-primes.</p> <p>$2q^2 = p^2 \Rightarrow p^2$ is divisible by 2 $\Rightarrow p$ is divisible by 2</p> <p>$\Rightarrow p = 2a$, where 'a' is some integer ----- (i)</p> <p>$4a^2 = 2q^2 \Rightarrow q^2 = 2a^2 \Rightarrow q^2$ is divisible by 2 $\Rightarrow q$ is divisible by 2</p> <p>$\Rightarrow q = 2b$, where 'b' is some integer ----- (ii)</p> <p>(i) and (ii) leads to contradiction as 'p' and 'q' are co-primes.</p> <p>$\therefore \sqrt{2}$ is an irrational number.</p>	$\frac{1}{2}$ 1 $\frac{1}{2}$ 1
	SECTION D	

	This section comprises of Long Answer (LA) type questions of 5 marks each.	
32(A).	The sum of first seven terms of an A.P. is 182. If its 4 th term and the 17 th term are in the ratio 1 : 5, find the A.P.	
Sol.	<p>Let a be the first term and d be the common difference.</p> $S_7 = 182 \Rightarrow \frac{7}{2}(2a + 6d) = 182 \quad 1$ $\Rightarrow 2a + 6d = \frac{182 \times 2}{7} = 52$ $a + 3d = 26 \quad \text{----- (i)} \quad 1$ $\frac{a_4}{a_{17}} = \frac{1}{5} \Rightarrow \frac{a + 3d}{a + 16d} = \frac{1}{5} \Rightarrow 5a + 15d = a + 16d \quad 1$ $4a = d \quad \text{-----(ii)} \quad \frac{1}{2}$ <p>Solving (i) and (ii)</p> $a = 2 \text{ and } d=8 \quad \frac{1}{2} + \frac{1}{2}$ $\therefore \text{AP is } 2, 10, 18, 26, \dots \quad \frac{1}{2}$	
	OR	
32(B).	The sum of first q terms of an A.P. is $63q - 3q^2$. If its p th term is -60, find the value of p. Also, find the 11 th term of this A.P.	
Sol.	$S_q = 63q - 3q^2$	

	$\therefore S_1 = 60 \Rightarrow a_1 = 60$ (1 st term)	1
	$S_2 = 63(2) - 3(2)^2 = 126 - 12 = 114$	
	$a_1 + a_2 = 114 \Rightarrow a_2 = 114 - 60 = 54$	1
	$d = a_2 - a_1 = 54 - 60 = -6$	1
	$a_p = -60$	
	$60 + (p-1)d = -60$	
	$(p-1)(-6) = -120 \Rightarrow p = 21$	1
	$a_{11} = a + 10d = 60 + 10(-6) = 0$	1
33(A).	Prove that a parallelogram circumscribing a circle is a rhombus.	
Sol.	<p>ABCD is a parallelogram touching the circle at P, Q, R, S by sides AB, BC, CD, DA respectively.</p> 	
	We know that tangents drawn from the external point to a circle are equal.	1 for correct figure
	$\therefore AP = AS$ ----- (i)	

PB = BQ	----- (ii)	2
CR = CQ	----- (iii)	1
DR = DS	----- (iv)	1
	Adding (i), (ii), (iii), (iv)	
	$(AP + PB) + (CR + DR) = (AS + DS) + (BQ + CQ)$	
	$AB + CD = AD + BC$	
	ABCD is a parallelogram	$\frac{1}{2}$
	$\Rightarrow AB = CD, AD = BC$	
	$\Rightarrow 2AB = 2AD \Rightarrow AB = AD$	$\frac{1}{2}$
	$\Rightarrow ABCD$ is a rhombus.	
	OR	
33(B)	(B)	
		<p>In the given figure, tangents PQ and PR are drawn to a circle such that $\angle RPQ = 30^\circ$. A chord RS is drawn parallel to the tangent PQ. Find the measure of $\angle RQS$.</p>

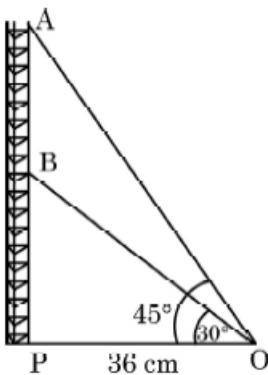
Sol.	<p>$PQ = PR$ (tangents drawn from an external point to the circle)</p> $\therefore \angle PQR = \angle PRQ$ <p>In $\triangle PQR$, $\angle PQR = \angle PRQ = \frac{1}{2}(180^\circ - 30^\circ) = 75^\circ$</p> <p>Draw a perpendicular QL from Q to QP</p> <p>Now, $\angle PQL = 90^\circ$</p> <p>$\therefore \angle RQL = 90^\circ - 75^\circ = 15^\circ$</p> <p>$\triangle RQL \cong \triangle SQL$ (SAS)</p> <p>$\therefore \angle RQL = \angle SQL = 15^\circ$</p> <p>$\therefore \angle RQS = 15^\circ + 15^\circ = 30^\circ$</p>	1 1 1 1 1 1 1 1																												
34.	<p>250 apples of a box were weighed and the distribution of masses of the apples is given in the following table :</p> <table border="1" data-bbox="203 1087 1127 1185"> <thead> <tr> <th>Mass (in grams)</th><th>80 – 100</th><th>100 – 120</th><th>120 – 140</th><th>140 – 160</th><th>160 – 180</th></tr> </thead> <tbody> <tr> <th>Number of apples</th><td>20</td><td>60</td><td>70</td><td>x</td><td>60</td></tr> </tbody> </table> <p>(i) Find the value of x and the mean mass of the apples. 3</p> <p>(ii) Find the modal mass of the apples 2</p>	Mass (in grams)	80 – 100	100 – 120	120 – 140	140 – 160	160 – 180	Number of apples	20	60	70	x	60																	
Mass (in grams)	80 – 100	100 – 120	120 – 140	140 – 160	160 – 180																									
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Sol.	<p>(i) $20 + 60 + 70 + x + 60 = 250$</p> $x = 250 - 210 = 40$ <table border="1" data-bbox="203 1407 1174 1623"> <thead> <tr> <th>Mass</th><th>80 – 100</th><th>100 – 120</th><th>120 – 140</th><th>140 – 160</th><th>160 – 180</th><th>Total</th></tr> </thead> <tbody> <tr> <td>No. of apples f_i</td><td>20</td><td>60</td><td>70</td><td>$x = 40$</td><td>60</td><td>250</td></tr> <tr> <td>x_i</td><td>90</td><td>110</td><td>130</td><td>150</td><td>170</td><td></td></tr> <tr> <td>$x_i f_i$</td><td>1800</td><td>6600</td><td>9100</td><td>6000</td><td>10200</td><td>33700</td></tr> </tbody> </table> <p>Mean mass $= \frac{33700}{250} = 134.8$</p>	Mass	80 – 100	100 – 120	120 – 140	140 – 160	160 – 180	Total	No. of apples f_i	20	60	70	$x = 40$	60	250	x_i	90	110	130	150	170		$x_i f_i$	1800	6600	9100	6000	10200	33700	1 1 1 for correct table 1
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	<p>Mean mass = 134.8 g</p> <p>(ii) Modal class = 120-140</p> $\text{Mode} = 120 + \frac{(70 - 60)}{(140 - 60 - 40)} \times 20$ $= 125$ <p>Hence modal mass = 125 g</p>	$\frac{1}{2}$ 1 $\frac{1}{2}$
35.	A solid is in the shape of a right-circular cone surmounted on a hemisphere, the radius of each of them being 7 cm and the height of the cone is equal to its diameter. Find the volume of the solid.	
Sol.	<p>Radius of cone = radius of hemisphere = 7 cm</p> <p>\therefore Height of cone = 14 cm</p> <p>Volume of solid = Volume of hemisphere + volume of cone</p> $= \frac{2}{3}\pi(7)^3 + \frac{1}{3}\pi(7)^2 14$ $= \frac{1}{3} \times \frac{22}{7} \times 7 \times 7(14 + 14)$ $= \frac{154}{3} \times 28 = \frac{4312}{3} \text{ cm}^2 \text{ or } 1437.33 \text{ cm}^2$ 	1 $1\frac{1}{2} + 1\frac{1}{2}$ 1
	<p>SECTION E</p> <p>This section comprises of 3 case-study based questions of 4 marks each.</p>	

36.

Radio towers are used for transmitting a range of communication services including radio and television. The tower will either act as an antenna itself or support one or more antennas on its structure. On a similar concept, a radio station tower was built in two Sections A and B. Tower is supported by wires from a point O.

Distance between the base of the tower and point O is 36 cm. From point O, the angle of elevation of the top of the Section B is 30° and the angle of elevation of the top of Section A is 45° .



Based on the above information, answer the following questions :

- Find the length of the wire from the point O to the top of Section B.
- Find the distance AB.

OR

Find the area of $\triangle OPB$.

- Find the height of the Section A from the base of the tower.

Sol.

$$(i) \quad \text{In } \triangle OBP, \cos 30^\circ = \frac{OP}{OB}$$

$$\frac{\sqrt{3}}{2} = \frac{36}{OB} \Rightarrow OB = \frac{72}{\sqrt{3}} \\ = 24\sqrt{3} \text{ cm}$$

$\frac{1}{2}$

$\frac{1}{2}$

$$(ii) \text{In } \Delta OBP, \tan 30^\circ = \frac{PB}{36} \Rightarrow PB = \frac{36}{\sqrt{3}}$$

$$PB = 12\sqrt{3}$$

1

$$\text{In } \Delta OAP, \tan 45^\circ = \frac{AP}{36} \Rightarrow AP = 36 \text{ cm}$$

$\frac{1}{2}$
 $\frac{1}{2}$
 $\frac{1}{2}$

$$AB = AP - PB = 36 - 12\sqrt{3} = 12(3 - \sqrt{3}) \text{ cm}$$

OR

$$(ii) \text{Area of } \Delta OPB = \frac{1}{2} \times OP \times PB$$

$$= \frac{1}{2} \times 36 \times 12\sqrt{3} = 216\sqrt{3} \text{ cm}^2$$

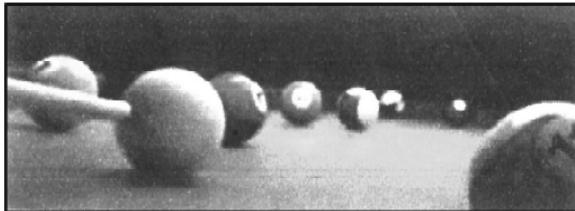
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$$(ii) \quad AP = 36 \text{ cm}$$

1

37.

“Eight Ball” is a game played on a pool table with 15 balls numbered 1 to 15 and a “cue ball” that is solid and white. Of the 15 numbered balls, eight are solid (non-white) coloured and numbered 1 to 8 and seven are striped balls numbered 9 to 15.



The 15 numbered pool balls (no cue ball) are placed in a large bowl and mixed, then one ball is drawn out at random.

Based on the above information, answer the following questions :

- What is the probability that the drawn ball bears number 8 ?
- What is the probability that the drawn ball bears an even number ?

OR

What is the probability that the drawn ball bears a number, which is a multiple of 3 ?

- What is the probability that the drawn ball is a solid coloured and bears an even number ?

Sol.

$$(i) P(\text{drawing ball bearing number 8}) = \frac{1}{15}$$

1

$$(ii) \text{Even numbers} = 2, 4, 6, 8, 10, 12, 14$$

 $\frac{1}{2}$

$$\text{No. of favourable outcomes} = 7$$

$$P(\text{even number}) = \frac{7}{15}$$

 $1\frac{1}{2}$

OR

$$(ii) \text{Multiples of 3 are } 3, 6, 9, 12, 15$$

 $\frac{1}{2}$

$$\text{No. of favourable outcomes} = 5$$

	$\therefore P(\text{multiple of 3}) = \frac{5}{15} = \frac{1}{3}$ <p>(iii) Solid colour and even number 2, 4, 6, 8</p> $P(\text{solid colour and bear an even no.}) = \frac{4}{15}$	$1\frac{1}{2}$
38.	<p>A coaching institute of Mathematics conducts classes in two batches I and II and fees for rich and poor children are different. In batch I, there are 20 poor and 5 rich children, whereas in batch II, there are 5 poor and 25 rich children. The total monthly collection of fees from batch I is ₹ 9000 and from batch II is ₹ 26,000. Assume that each poor child pays ₹ x per month and each rich child pays ₹ y per month.</p>  <p>Based on the above information, answer the following questions :</p> <ol style="list-style-type: none"> Represent the information given above in terms of x and y. Find the monthly fee paid by a poor child. <p style="text-align: center;">OR</p> <p>Find the difference in the monthly fee paid by a poor child and a rich child.</p> <ol style="list-style-type: none"> If there are 10 poor and 20 rich children in batch II, what is the total monthly collection of fees from batch II ? 	1
Sol.	$(i) 20x + 5y = 9000$ $5x + 25y = 26000$	1

<p>(ii) Solving the equations $x = 200$, $y = 1000$</p> <p>Monthly fee paid by poor child = ₹200</p> <p>OR</p> <p>(ii) getting $x=200$ and $y= 1000$</p> <p>Difference in the fee = $1000 - 200 = ₹ 800$</p> <p>(iii) $10x + 20y = 10(200) + 20(1000)$</p> <p>$= ₹ 22000$</p>	<p>2</p> <p>$1 + \frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>1</p>
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